# CERTIFICATION AND EXCHANGE IN VERTICALLY CONCENTRATED MARKETS

Konrad Stahl (Mannheim) Roland Strausz (Berlin)

### Motivation

2005: Biggest loss of Mercedes Car Group Quality problems braking systems Repair-costs: 500 Million Euro (680.000 cars) Quality problems battery control unit software 1.3 million cars Reputation cost: laughing stock in Germany Parts delivered by BOSCH quality management of supplied goods

#### Kein Ruhmesblatt Rückrufe in Deutschland,



## Motivation

Recalls in automobile industry due to increased outsourcing
 Informational asymmetries between upstream and downstream producer
 Role for external certification

Startoete | Suche | Upersiont | Kontala | Impressum | Englis



#### Motivation EDAG: independent certifier of car modules and systems Strömungsprüfstände Kontakte Interview: one of seven certifiers worldwide **Prüttechnik** Thomas Schuster holds a dominant, if not exclusive, market position in a number of components > e-mail rodukte large economies of scope in certification In unseren Stiomungsprüfständen erzeugen wir definierte und reproduzierbare Strömungszustände Differenzdruck simuliert und im zweiten Schritt die Auswirkungen der Strömungen auf das Bauteil Zylinderköpfe Luftmassenmesser

## Motivation

Role of certification in a bilateral monopoly?



## Model

- Seller:  $Pr{q_h} = \lambda$ ;  $Pr{q_l} = 1 \lambda$  with  $q_h > q_l$
- Production cost quality  $q_i$  is  $c_i$ , where  $c_h > c_l = 0$
- □ Lemons problem:  $c_h > q^e = \lambda q_h + (1 \lambda) q_l$
- With asymmetric information q<sub>h</sub>-seller does not sell his good
- Certification: An external certifier can reveal the sellers quality credibly at a cost c<sub>c</sub>
  - q<sub>h</sub>-seller has a demand for certification
  - buyer has a demand for certification

## **The Game**

#### **Buyer certification**

- 1. Certifier sets p<sub>c</sub>
- 2. Nature picks q<sub>i</sub>
- 3. Seller sets price p
- 4. Buyer decides to buy certification
- 5. Buyer decides about buying the good

#### Questions:

1.Which game does the certifier like better?2.Which game delivers higher social welfare?3.What are the driving differences behind the two models?

#### Seller certification

- 1. Certifier sets p<sub>c</sub>
- 2. Nature picks q<sub>i</sub>
- 3. Seller sets price p
- 4. Seller decides to buy certification
- Buyer decides about buying the good

## **Results/Intuition**

#### **Buyer certification**

- Certification is an inspection device
- Inspection game
- Mixed equilibrium
- Both goods are certified with positive prob.
- q<sub>I</sub> good sometimes not sold in EQ
- Inefficient

#### Seller certification

- Certification is a signaling device
- Signaling game
- Pure equilibrium
- Only q<sub>h</sub> goods are certified
- All goods are sold in EQ
- Efficient

## **Buyer certification**

Optimal pricing behavior certifier?
 Inspection device: Buyer certifies to prevent cheating
 Demand for certification high when

 Buyer's uncertainty about quality is large: μ=1/2
 Intermediate price of the good: p=(q<sub>h</sub>+q<sub>l</sub>)/2

 Certifier tries to induce this outcome

## **Buyer certification**

- Buyer's strategy: certifying and buying
  - 1. **s<sub>nb</sub>: no certification, always buying**
  - 2. s<sub>nn</sub>: no certification, no buying
  - 3. s<sub>ch</sub>: certify, buy only h quality
  - 4. Scol cortify, always buy
  - 5. Oct Cortify, buy only I quality
- Decision conditional on  $p_c$ , p, and belief  $\mu$

p∧ q<sub>h</sub>

 $U(s_{nb}) = \mu q_{h} + (1 - \mu)q_{l} - p$ 

U(s<sub>nn</sub>)=0

 $U(s_{nb}) = \mu q_{h} + (1 - \mu)q_{l} - p$ 

U(s<sub>nn</sub>)=0



 $U(s_{nb}) = \mu q_h + (1 - \mu) q_l - p$ 

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 $U(s_{nb}) = \mu q_{h} + (1 - \mu) q_{l} - p$ 

U(s<sub>nn</sub>)=0

U(s<sub>ch</sub>)=µ(q<sub>h</sub>-p)-p<sub>c</sub>



 $U(s_{nb}) = \mu q_{h} + (1 - \mu)q_{l} - p$ 

U(s<sub>nn</sub>)=0



 $U(s_{nb}) = \mu q_{h} + (1 - \mu)q_{l} - p$ 

 $U(s_{nn})=0$ 

 $U(s_{ch})=\mu(q_{h}-p)-p_{c}$ 



$$\begin{split} & \underbrace{\text{Willingness to pay for certification}}_{\Delta U_1 = U(s_{ch}) - U(s_{nb}) = \mu(q_h - p) - (q^e - p)} \\ & \Delta U_2 = U(s_{ch}) - U(s_{nn}) = \mu(q_h - p) \\ & \text{Buyer's willingness to pay: min} \{ \Delta U_1, \Delta U_2 \} \\ & \max_{(p,\mu)} \min\{ \Delta U_1, \Delta U_2 \} \qquad p = (q_h + q_l)/2; \ \mu = 1/2 \end{split}$$

 $U(s_{nb}) = \mu q_{h} + (1 - \mu)q_{l} - p$ 

U(s<sub>nn</sub>)=0



#### **Buyer certification equilibrium**

 $U(s_{nb}) = \mu q_{h} + (1 - \mu)q_{l} - p$ 

U(s<sub>nn</sub>)=0

 $U(s_{ch})=\mu(q_{h}-p)-p_{c}$ 



Result: Given  $\mu > \lambda$  and an equilibrium refinement (**q**, **0**) together with (**p**, **µ**) is the unique equilibrium outcome:

- q<sub>h</sub>-seller always sets price p
- q<sub>l</sub>-seller randomizes between price q<sub>l</sub> and p
- upon seeing price p, buyer certifies at random

## Details

Lemma: In any PBE  $(\sigma_l^*, \sigma_h^*, \mu^*, \sigma^*)$  of the subgame  $\Gamma(p_c)$  we have i)  $\sigma_l^*(p) = 0$  for all  $p \notin [q_l, q_h]$ ii)  $\sigma_h^*(p) = 0$  for all  $p < q_l$ ; iii)  $\Pi_l^* \ge q_l$ ; iv)  $\Pi_h^* < q_h - c_h$ .

Refinement: A Perfect Bayesian Equilibrium  $(\sigma_h^*, \sigma_l^*, \mu^*, \sigma^*)$  satisfies the Belief Restriction if, for any  $\mu \in (0, 1]$  and any out–of–equilibrium price p, we have

 $\Pi_l(p,\mu) < \Pi_l^* \land \Pi_h(p,\mu) > \Pi_h^* \Rightarrow \mu^*(p) \ge \mu.$ 

Bester&Ritzberger(2001); extends Cho-Kreps: μ=1

Lemma: Any Perfect Bayesian Equilibrium  $(\sigma_l^*, \sigma_h^*, \mu^*, \sigma^*)$  of the subgame  $\Gamma(p_c)$  that satisfies B.R. exhibits

i) 
$$\sigma_h^*(p) = 0$$
 for all  $p < \tilde{p}$ ;  
ii)  $\Pi^* > \tilde{p}$ 

1) 
$$\Pi_h^* \ge p - c_h$$

# **Optimal p**<sub>c</sub> buyer certification



# Optimal p<sub>c</sub> buyer certification





 $□ p_c = \Delta q/4$  □ actual randomization

## **Seller certification**

q<sub>h</sub>-seller certifies to prove q<sub>h</sub> and price p=q<sub>h</sub>.
Π<sub>h</sub>(p<sub>c</sub>)=q<sub>h</sub>-c<sub>h</sub>-p<sub>c</sub>
Π<sub>l</sub>(p<sub>c</sub>)=q<sub>l</sub>
Optimal p<sub>c</sub>=q<sub>h</sub>-c<sub>h</sub>
In Eq: Π<sub>h</sub>=0; Π<sub>l</sub>=q<sub>l</sub>
Π<sub>c</sub>=λ(q<sub>h</sub>-c<sub>h</sub>-c<sub>c</sub>)

### Comparison

- Certifier's profit larger with seller certification.
- Welfare?
  - no certification
    - q<sub>h</sub> good not sold / no certification costs
  - buyer certification
    - q good not always sold / probabilistic certification
  - seller certification
    - All goods always sold / probabilistic certification
  - buyer certification maximizes welfare

## Conclusions

- Certification by informed party better for
  - certifier
  - welfare
  - no need for governmental intervention
- Certification by informed party:
  - signaling high quality
- Certification by uninformed party:
  - inspection game