Session: (June $4^{\text {th }}-$ Product Differentiation - Applied)

# "VERTICAL CONTRACTS BETWEEN MANUFACTURERS AND RETAILERS: INFERENCE WITH LIMITED DATA" 

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## MOTIVATION

## - Why do we care?

Efficiency
Double Marginalization or more efficient contracting?

Competition

Balance of power

Beyond IO,
Modeling retailer behavior, e.g. Price dynamics (Chevalier, Kashyap, Rossi, AER, 2003)
International Economics (cost pass-through)

- Why is it difficult to analyze?

Limited data observability (wholesale prices, costs)

Non-marginal components

## MAIN CONTRIBUTION

- Present method to analyze degree of competitive interactions between manufacturers and retailers (vertical contracts) even when wholesale prices are unobserved
- Apply methodology to a certain market (yogurt)


## GENERAL STRATEGY

- Estimate brand-store level demand (using flexible functional form)
- Given demand estimates, compute price-cost margins (PCM) for retailers and manufacturers implied by different supply models (without observing wholesale prices)

Each model implies different PCM for retailers and manufacturers

- Test between different supply models by asking which set of implied PCM is more compatible with "observed" PCM (using non-nested tests)


## CONCLUSIONS

- Model that best fits the data:

Marginal wholesale price close to marginal cost and retail price is the unconstrained profit-maximizing price

- Able to rule out Double Marginalization model
- Consistent with several scenarios, for example:

1. Retailers have large bargaining power
2. Non-linear pricing by manufacturers

Two-part tariffs
Quantity discounts
3. Others...

## OUTLINE

- Related literature
- Illustrative example
- The models (demand and supply)
- Estimation method
- Testing between supply models
- The data
- The yogurt market
- Results
- Conclusions and Extensions


## RELATED LITERATURE

- Extensive theoretical work on vertical contracts

For a survey see Katz (1989).

- Empirical work:

Bresnahan and Reiss (1985)
Corts (2000)
Mortimer (2002)
Closer to this paper:
Messinger and Narasimhan (95)
Chintagunta, Bonfer and Song (2000)
Kadiyali, Chintagunta and Vilcassim (2000)
Main differences: use data on wholesale prices, just one retailer.

- Tests of vertical pricing models (very few):

Sudhir (2001), Villas-Boas and Zhao (2001)
Main difference: just one retailer.

## ILLUSTRATIVE EXAMPLE



## SUPPLY MODELS CONSIDERED

- Simple Linear Pricing $\Rightarrow$ Double Marginalization
- Vertically Integrated
- Alternative (Strategic) models:

Non-linear pricing (2 "special/extreme" cases)
Wholesale pricing at marginal cost
Retail margin close to zero
Retailers vertically integrated in private labels
Manufacturer level collusion
Retail level collusion

## THE SUPPLY MODELS

| MODEL | Manufacturers: m | Retailers: r |
| :---: | :---: | :---: |
| Simple Linear Pricing | $\max _{\mathrm{p}^{\mathrm{w}}} \pi_{\mathrm{mj}} \text { given } \mathrm{p}\left(\mathrm{p}^{\mathrm{w}}\right)$ | $\max _{\mathrm{p}} \pi_{\mathrm{rj}}$ |
| Zero wholesale margin | $\mathrm{p}^{\mathrm{w}}=\mathrm{c}^{\mathrm{w}}$ | $\max _{\mathrm{p}} \pi_{\mathrm{rj}}$ |
| Zero retail margin | $\max _{\mathrm{p}^{\mathrm{w}}} \pi_{\mathrm{mj}}$ | $\mathrm{p}=\mathrm{p}^{\mathrm{w}}+\mathrm{c}^{\mathrm{r}}$ |
| Private Label | $\begin{gathered} \mathrm{p}^{\mathrm{w}}=\mathrm{c}^{\mathrm{w}}, \text { for } \mathrm{j}=\text { private label } \\ \quad \text { and otherwise } \\ \max _{\mathrm{p}^{\mathrm{w}}} \sum_{\mathrm{j}} \pi_{\mathrm{mj}} \text { given } \mathrm{p}\left(\mathrm{p}^{\mathrm{w}}\right) \end{gathered}$ | $\underset{\mathrm{p}}{\operatorname{Max}} \pi_{\mathrm{rj}}$ |
| Manufacturer collusion | $\max _{\mathrm{p}^{\mathrm{w}}} \sum_{\mathrm{j}} \pi_{\mathrm{mj}} \text { given } \mathrm{p}\left(\mathrm{p}^{\mathrm{w}}\right)$ | $\underset{\mathrm{p}}{\operatorname{Max}} \pi_{\mathrm{rj}}$ |
| Retail collusion | $\max _{\mathrm{p}^{\mathrm{w}}} \pi_{\mathrm{mj}} \text { given } \mathrm{p}\left(\mathrm{p}^{\mathrm{w}}\right)$ | $\max _{\mathrm{p}} \sum_{\mathrm{j}} \pi_{\mathrm{rj}}$ |
| Joint profit maximizing | $\max _{\mathrm{p}} \sum_{\mathrm{j}} \pi_{\mathrm{j}}$ |  |

## SIMPLE LINEAR PRICING MODEL

- Manufacturers set wholesale prices and then given the wholesale prices retailers set retail prices
- $\operatorname{Max} \pi_{r t}=\sum_{j \in \operatorname{Srt}}\left[p_{j t}-p^{w}{ }_{j t}-c^{r}{ }_{j t}\right] s_{j t}(p)-F C$
$\Rightarrow s_{j t}+\sum_{k \in S i t}\left[p_{k t}-p^{w}{ }_{k t}-c^{r}{ }_{k t}\right] \partial_{k t}(p) / \partial p_{j t}=0, j=1, \ldots N$.

Define
$T_{r}: T_{r}(i, j)=1$ when $i, j \in S_{r t}$ and 0 otherwise
$\Delta_{r}$ is a matrix of cross-price elasticities of demand

Solving for the PCM of the retailers

$$
\begin{equation*}
p-p^{w}-c^{r}=-\left(T_{r}, \Delta_{r}\right)^{-1} s(p) \tag{1}
\end{equation*}
$$

- Manufacturers

$$
\operatorname{Max} \pi_{w t}=\sum_{j \in S w t}\left[p_{j t}^{w}-c^{w}{ }_{j t}\right] s_{j t}(p)-F C^{w}
$$

given that retailers price according to

$$
\begin{equation*}
p-p^{w}-c^{r}=-\left(T_{r}, \Delta_{r}\right)^{-1} s(p) \tag{1}
\end{equation*}
$$

Rearranging the first order conditions, to solve for the PCM of the manufacturers (in matrix notation)

$$
\begin{equation*}
p^{w}-c^{w}=-\left(T_{w} \cdot \Delta_{w}\right)^{-1} s(p) \tag{2}
\end{equation*}
$$

where
$T_{w}(i, j)=1$ when $i, j \in S_{w t}$ and 0 otherwise and $\Delta_{w}$ has the cross-price elasticities of derived demand (has also effect of cost pass-through).

Note: $\boldsymbol{S}_{w t} \neq \boldsymbol{S}_{r t}$.

- The PCM for the other models are obtained from (1) and (2).


## DEMAND MODEL

- Discrete choice model for differentiated products
- Indirect latent utility from consumer $i$ choosing product $j$ (brand-store) at time $t$

$$
U_{i j t}=D_{t}+d_{j}+x_{j t} \beta_{i}-\alpha_{i} p_{j t}+\xi_{j t}+\varepsilon_{i j t}
$$

$d_{j}$ product dummy variables, $\mathrm{D}_{\mathrm{t}}$ seasonal dummies
$x_{j t}$ observed product characteristics
$\varepsilon_{i j t}$ distribution of consumer preferences about unobserved product characteristics (will be integrated out)

- What is in $\xi_{j t}$ ? Changes in
-unobserved consumer preferences
-other unobserved market specific conditions
(e.g. unobserved promotions, previous sales, changes in shelf display)
- Specifying consumer heterogeneity
$\left|\begin{array}{c}\alpha_{i} \\ \beta_{i}\end{array}\right|=\left|\begin{array}{lll}\alpha \\ \beta\end{array}\right|+\Phi_{D} \quad D_{i}+\Phi_{v} \quad v_{i}$
$D_{i}$ observed and $v_{i}$ unobserved consumer characteristics

Note: if $\alpha=\alpha_{i}$ and $\beta=\beta_{i}($ and $\varepsilon$ extreme value $) \Rightarrow$ Logit.

- Consumer purchases one unit of the good that gives the highest utility conditional on characteristics, prices and outside good.
- Aggregate market share of product $j$
$s_{j t}=\int_{\left(\left\{\left(D_{i}, v_{i}, \varepsilon_{i}\right) \mid U_{i j t} \geq U_{i h t} h=0, \ldots N\right\}\right) d F(\varepsilon) d F(v) d F(D), ~(1)}$


## DEMAND ESTIMATION

- Estimate demand parameters that produce predicted aggregate market shares close to observed ones
- Data requirements:

Prices in different markets (weeks)
Aggregate market shares
Product characteristics
Consumer characteristics

- Problem of estimation - prices are correlated with $\xi_{j t}$
- Solution: Use instruments for prices
- Need instruments with product level variation
- I use two instrumental variable (IV) specifications:

1. Manufacturer level input prices interacted with brandstore dummy variables \& Retail level input prices
2. Manufacturer-level input prices interacted with brand dummy variables \& Retail level input prices

## TESTING THE SUPPLY MODELS

## 1. Test of each supply model:

- Starting with the accounting identity obtained by adding up the implied PCM

$$
p-c^{w}-c^{r}=P C M_{r}+P C M_{w}
$$

- Having information on costs $\left(c^{r}+c^{w}\right)$ I can compare the implied PCM with PCM obtained from estimates of cost.

This reduces to estimating the supply pricing equation

$$
p=c \gamma+P C M_{r} \lambda_{r}+P C M_{w} \lambda_{w}+\varepsilon
$$

and to test if the $\lambda$ are jointly significantly different from 1
2. Comparing different supply models:

- Models are not particular cases of other models
- Non-nested testing procedures

Intuition: Given a null model how "likely" is the alternative model?

## THE DATA

- Scanner data collected at several retail stores in two markets over two years - Source: IRI

Weekly UPC-store level data on prices and quantities for 24 product categories (used yogurt category)

- Demographics at Zip Code level - Source: Census 1990
- Product characteristics - Source: Label reads


## THE INPUT DATA

## - Manufacturer level input prices

## Input Prices

-Citric acid
-Plastic
-Sugar
-Non-fat Grade A milk
-Whey Protein
-Strawberry
-Interest rate
-Wages

- Ohio (plant Dannon)
- Illinois (plant Kraft, Private Label store 3, retailers)
- Michigan (plant Yoplait)
- Oregon (plant Private Label store 2)
-Gasoline prices
-Industrial energy prices
Petroleum Marketing Monthly
for states OH,IL,MI, OR
- Retail level input prices

Input Prices

- Real Estate Indices
- Commercial energy prices
- Chain size

Number employees
Number stores

- Gasoline prices

Sources

CB Richard Ellis
EIA - 826, Table 53
Human Resources Chains
Human Resources Chains
Petroleum Markt. Monthly

## YOGURT MARKET

- Why yogurt?

Short time storable good (ignore dynamic aspects)
Not heavily promoted by retailers (implications for IV)
Small number of key industry players
Reasonably established private labels

- Why should we care about yogurt?

Application of the general method to a local market

- Manufacturers

Dannon and General Mills (Yoplait) 62\% yogurt sales
Private labels $15 \%$
Kraft 5\%
All others have individual shares less than $2 \%$

- Retailers in local market

Three retail chains have jointly $75 \%$ sales

- Local market

Mid-west metropolitan area between 1991-93
2 Zip Code areas

## Store Location

## DATA

## - Definition of variables

Price: in cents per serving, 1 serving $=6$ ounce cup

| Mean | Median | Std | Min | Max | Brand <br> Variation | Week <br> Variation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | 48 | 9.2 | 24 | 72 | $68.3 \%$ | $2.4 \%$ |

Potential market: half a serving per capita a week
$\Rightarrow$ half the population in two Zip Code areas

International patterns (per capita servings/week)
Bulgaria: 3.4 (Lactobacillus bulgaricus)
France: 1.9 ; Germany: 1.2; USA: 0.53 ; Canada: 0.3

Market shares: servings sold / total potential servings

| Combined Shares | Mean | Min | Max |
| :--- | :---: | :---: | :---: |
| Dannon | $17 \%$ | $5 \%$ | $50 \%$ |
| General Mills | $9 \%$ | $4 \%$ | $31 \%$ |
| Store 1 | $2 \%$ | $1 \%$ | $9 \%$ |
| Store 2 | $20 \%$ | $58 \%$ | $10 \%$ |
| Store 3 | $13 \%$ | $7 \%$ | $24 \%$ |

## DATA

Outside good: products sold at other retailers

- Demographics

Median household income: US $\$ 30,000 /$ year
Median household size: 2.5 persons

- Product Characteristics

Store 2 dummy
Store 3 dummy
Total calories
Vitamin A and C content dummy
Calcium content
Aspartame content dummy
Available in different sizes dummy

## RESULTS

## - Demand

Results from Random Coefficients model

| Variable | Mean | Interaction with |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\log$ (Income) | Age | Unobserv. |
| Constant | $-7.9^{*}$ | 0.07 | 5.55 | 0.35 |
|  | $(0.25)$ | $(0.55)$ | $(1.43)$ | $(0.26)$ |
| Price | -5.69 | 1.25 | -2.43 | 0.93 |
|  | $(0.70)$ | $(0.28)$ | $(2.14)$ | $(0.48)$ |
| Store 2 | $3.03^{*}$ | 1.56 | -6.11 | 0.07 |
|  | $(0.04)$ | $(0.41)$ | $(0.55)$ | $(0.13)$ |
| Store 3 | $1.21^{*}$ | 1.43 | -5.54 | 0.15 |
|  | $(0.04)$ | $(0.51)$ | $(0.59)$ | $(0.15)$ |
| Calories | $-0.25^{*}$ | 0.002 | -0.006 | 0.08 |
|  | $(0.01)$ | $(0.002)$ | $(0.007)$ | $(0.05)$ |
| Calcium | $5.81^{*}$ | 0.44 | 0.25 | 0.28 |
|  | $(0.14)$ | $(0.16)$ | $(0.02)$ | $(0.11)$ |
| Aspartame | $-5.81^{*}$ |  |  |  |
|  | $(0.21)$ |  |  |  |
| Different | $4.65^{*}$ |  |  |  |
| Sizes | $(0.13)$ |  |  |  |

Standard errors are in parenthesis. Regression included brand dummy variables, seasonal dummy variables and allows for a nonlinear interaction of price with log income. * Estimates from minimum distance procedure.

## RESULTS

## - Demand - Are IV working?

First Stage
$\mathrm{R}^{2}=0.82$
Wald test $\{$ instruments' coefficients $=0\}=1809$ (421)
Sample coefficients (first stage)

| Product | Plastic | Milk | Wage IL | Wage MI |
| :---: | :---: | :---: | :---: | :---: |
| Retail Price | 0.006 | 0.128 | 0.031 | 0.015 |
| of Yoplait | $(0.002)$ | $(0.058)$ | $(0.012)$ | $(0.007)$ |
| Custard Low-fat |  |  | Retail | Plant Location |
| Fruit |  |  | Location |  |

## Alternative Specification

NNLS: not instrumenting for price

- coefficients change considerably
- PCM change also


## - Demand - Additional Specification Tests

1. set $v_{i}=0$ - estimates, PCM unchanged
2. robust to potential market definition
3. Demand specification with feature

IV versus OLS
PCM and ranking of models unchanged
Cannot reject exogeneity test for feature

## RESULTS

## - Demand - Price Elasticities

| Within store |
| :--- |
| Mean Cross Price Elasticity |
| Product Average |
| Store 1 Average |
| Store 2 Average |
| Store 3 Average |

## Example

|  | Changes in price of Dannon |  |
| :---: | :---: | :---: |
| Classic Fruit |  |  | Lowfat Plain

Across stores
Mean Cross Price Elasticity
Product Average 0.030
Store 1 Average 0.025
Store 2 Average 0.035
Store 3 Average 0.032

Persistent substitution patterns

## - Demand - flexible? Comparison to Logit

Overcome Logit restrictions in terms of cross-elasticities (Variance of cross-price elasticities is not zero)

## RESULTS

## - Price Cost Margins

| Model | Wholesale Margin |  | Retail Margin |  |
| :--- | :---: | :---: | :---: | :---: |
| Mean | Std | Mean | Std |  |
| Double <br> Marginalization | $38.3 \%$ | 8.2 | $37.9 \%$ | 8.7 |
| Zero wholesale <br> margin | 0 | 0 | $37.9 \%$ | 8.7 |
| Zero retail <br> margin | $37.3 \%$ | 8.0 | 0 | 0 |
| Vertical Integration <br> Private labels | $30.8 \%$ | 14.6 | $37.9 \%$ | 8.7 |
| Wholesale <br> collusion | $46.4 \%$ | 11.3 | $37.9 \%$ | 8.7 |
| Retail <br> collusion | $39.8 \%$ | 8.4 | $42.0 \%$ | 9.6 |
| Efficient vertical <br> pricing | Mean |  | Std |  |
|  | $42.0 \%$ |  | 9.6 |  |

## Recovered Costs

| Estimated <br> Costs / <br> Model | Percent | Negative |  | Std. <br> Dev. | Min |
| :--- | :--- | :--- | :--- | :--- | :--- | Max

## - Hypothesis Testing

Comparisons between models

## RESULTS

## - Non-Nested Tests

Intuition: Given a null model how likely is the alternative?

| Models | 1 | 2.1 | 2.2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Double Marginaliz. | - | $\mathbf{1 . 8 8}$ | 1.26 | 1.75 | 2.55 | 1.58 | 2.11 |
| 2.1 PCM $_{\mathrm{w}}=0$ | $\mathbf{0 . 9 3}$ | - | $\mathbf{0 . 1 6}$ | $\mathbf{0 . 5 8}$ | $\mathbf{0 . 6 8}$ | $\mathbf{0 . 8 5}$ | $\mathbf{0 . 1 2}$ |
| 2.2 PCM $_{\mathrm{r}}=0$ | 1.09 | $\mathbf{3 . 7 7}$ | - | 0.56 | 0.76 | 1.19 | 2.15 |
| 3 Private label | 0.40 | $\mathbf{3 . 2 6}$ | 0.16 | - | 0.39 | 0.28 | 2.08 |
| 4 Wholesale collusion | 2.05 | $\mathbf{1 . 8 8}$ | 0.55 | 1.15 | - | 1.06 | 2.29 |
| 5 Retail collusion | 0.99 | $\mathbf{4 . 0 4}$ | 2.43 | 0.58 | 0.82 | - | 2.13 |
| 6 Vertical efficient | 0.13 | $\mathbf{2 . 0 8}$ | 0.02 | 0.22 | 0.19 | 0.09 | - |

One side tests, critical value of 1.65 at $5 \%$ significance.

## Conclusions:

Model 2.1 provides the best fit

Results similar in alternative demand specifications

## EXTENSIONS / APPLICATIONS

- Extensions

1. Look at vertical contracts across different markets
2. Look at more than one category (in progress)

- Applications

1. Vertical merger analysis

Does a potential merger affect horizontal competition? Future project (dairy industry)
See also Manuszak (2001)
2. Pass-through of trade policies (tariffs, depreciations) Who absorbs most of policy change - foreign or domestic margins? (See Hellerstein, N,Y. Fed working paper, 2004)
3. Measure marginal cost advantages from exclusive dealing (see Asker, Harvard working paper, 2004)
4. Price discrimination:

Fair wholesale price legislation in Gasoline markets in California (as a motivation for future project)

Test for wholesale price discrimination (in progress)

## CONCLUSIONS

- Method to analyze vertical contracts without wholesale prices
- Empirical model of competing manufacturers' and retailers' decisions (related literature does not model retailers' decisions)
- Rule out Double Marginalization model
- Model that best fits the data:

Marginal wholesale pricing close to marginal cost and retailers choose profit-maximizing prices

- Consistent with several scenarios, for example:

1. Retailers having large bargaining power
2. Non-linear pricing by manufacturers

Two-part tariffs
Quantity discounts
3. Others...

