



# The Impact of Cap and Trade Regulation on Congested Electricity Market Equilibrium

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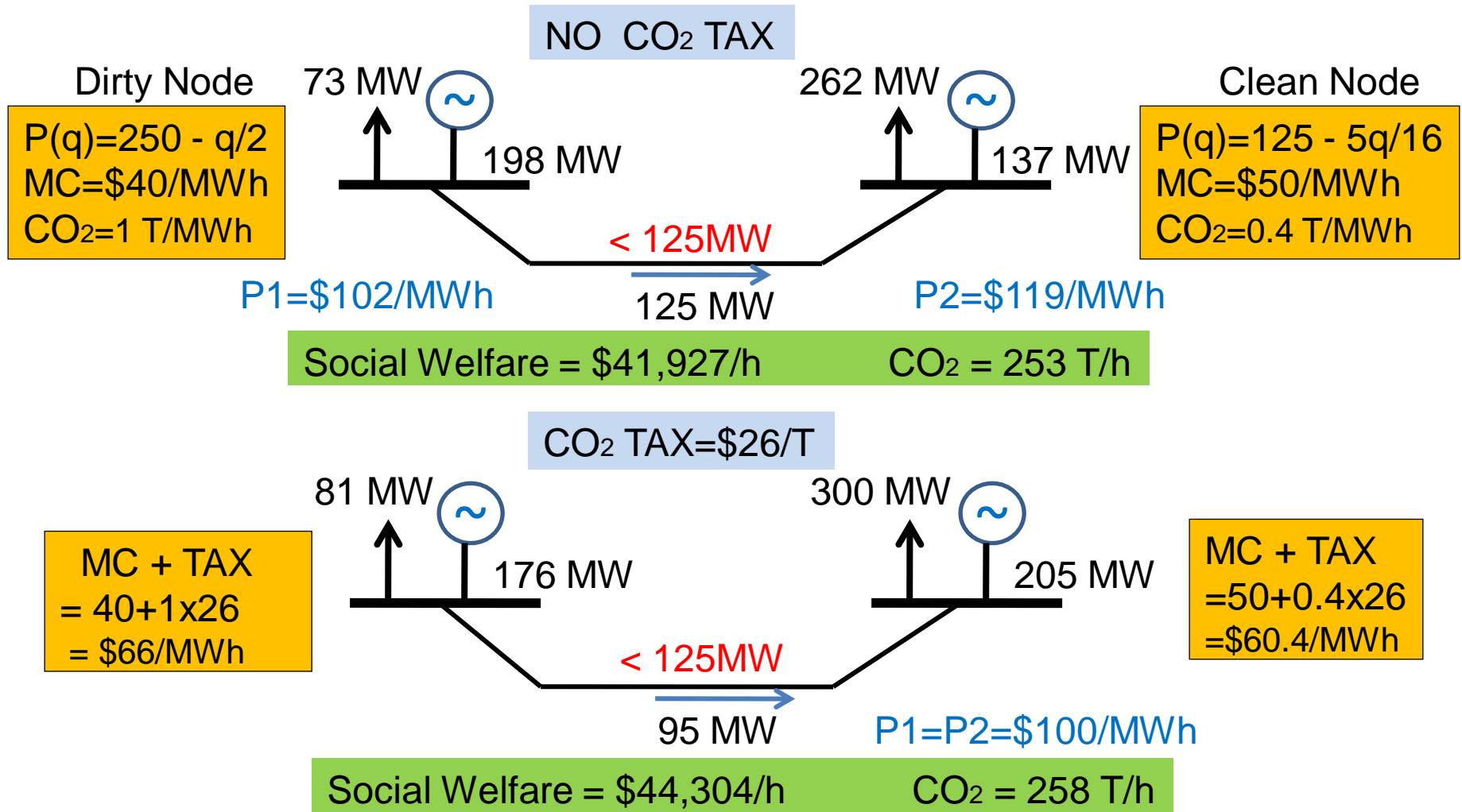
# Research on Regional GHG Regulation

- **Study of Leakage (displacement of emissions to areas with less restrictive regulation) and on contract shuffling based on zonal models**
- **Study of enforcement strategies (Source based vs. Load based)**
- **Study of impact on local industry**
- **Study of impact on grid operations and power markets**

# Factors affecting the efficacy of GHG regulation and its impact on the electric power system

- **Transmission network** (Network congestion effects and congestion management approach)
- **Specific form of GHG regulation** (Carbon Tax, Cap & Trade, Renewable Portfolio Standard (RPS), RECs, GHG allowances)
- **Demand response** (Demand elasticity, Metering and load control technology, Rate regulation, Business models, PHEV/EV penetration & smart charging technology)
- **Market structure** (Resource ownership and market rules) and strategic behavior of participants
- **Renewables integration** (economic incentives and dispatch policies)

# Example: Perverse Effect of Carbon Tax



Social Welfare = Consumer Surplus + Producers Profit + Congestion Rents + Tax

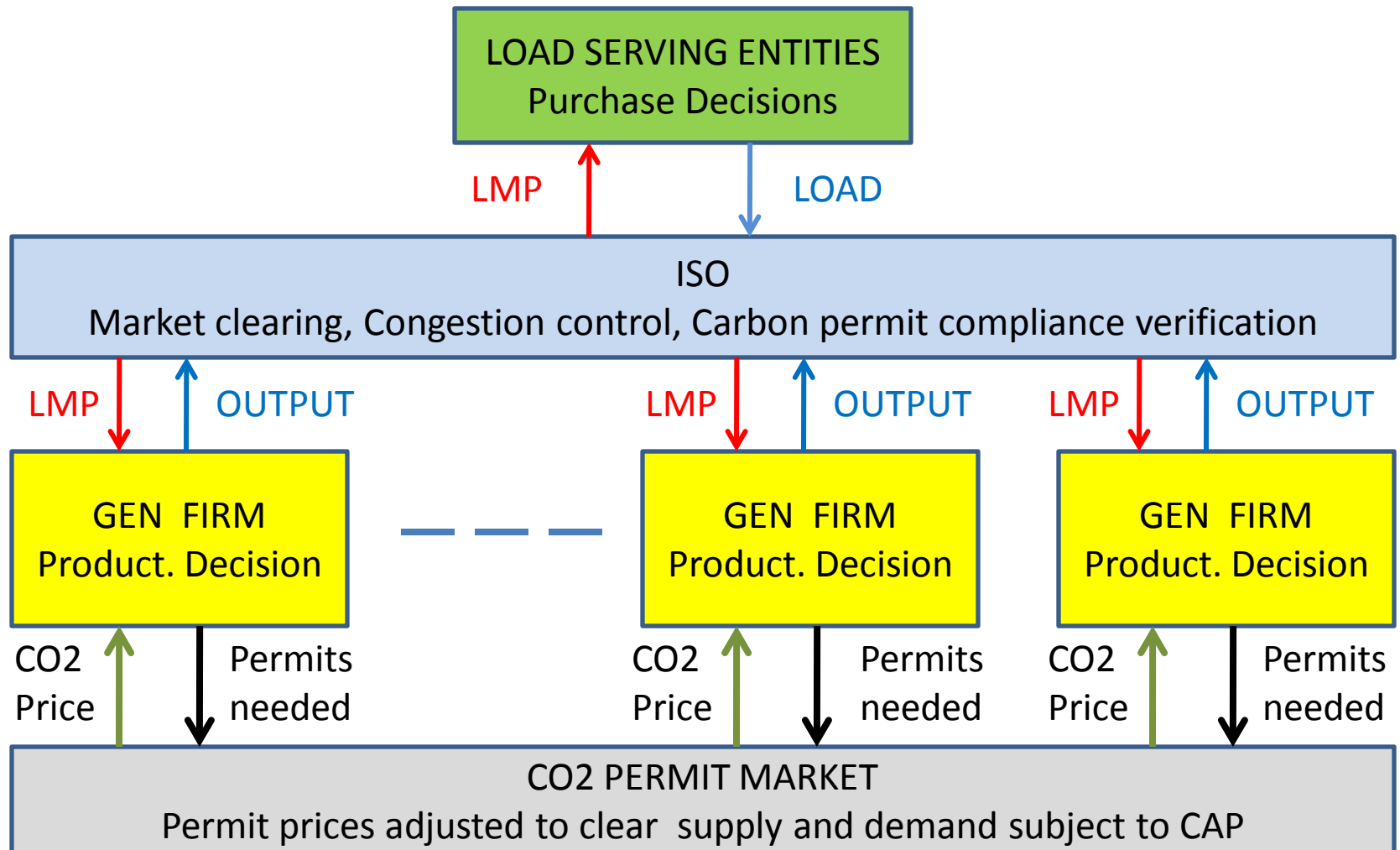
# Scope of this talk

- Describe an equilibrium model of an oligopoly electricity market in conjunction with a cap-and-trade policy to study the impact of such interactions.
- Demonstrate the potential impacts on market and environmental outcomes, and on the performance of the transmission system
  - For an IEEE 24-bus test network
  - For a reduced WECC 225-bus model of the Western Interconnect

# Equilibrium Model

- Transmission flows obey direct-current (DC) load flow model (Kirchhoff law) and are constrained by thermal limits (capacity of lines)
- Cournot producers with quadratic cost functions compete to sell energy at different locations in an LMP-based market and make output decisions so as to maximize profits.
- Demand is elastic and represented by nodal demand functions
- ISO clears the market and controls import/exports through locational congestion markups so as to maximize social welfare while satisfying security limits
- ISO monitors CO<sub>2</sub> permit compliance
- Endogenous CO<sub>2</sub> permit market sets carbon prices.

# Equilibrium Model with CO2 C&T



# Electric Power Network

$N$  = the set of buses

$L$  = the set of transmission lines

(MW = Megawatt)

$q_i$  MW output of the plant at bus  $i$

$r_i$  MW import/export at bus  $i$   
(import = +)

$load_i$  MW fixed load at bus  $i$

$K_l$  Rating of transmission line  $l$  (MVA)

$D_{l,i}$  PTDF $_{l,i}$  of line  $l$  with respect to  
a unit injection at bus  $i$  and  
a unit withdrawal at the slack bus

$\underline{q}_i$  Plant  $i$ 's must-run limit (MW)

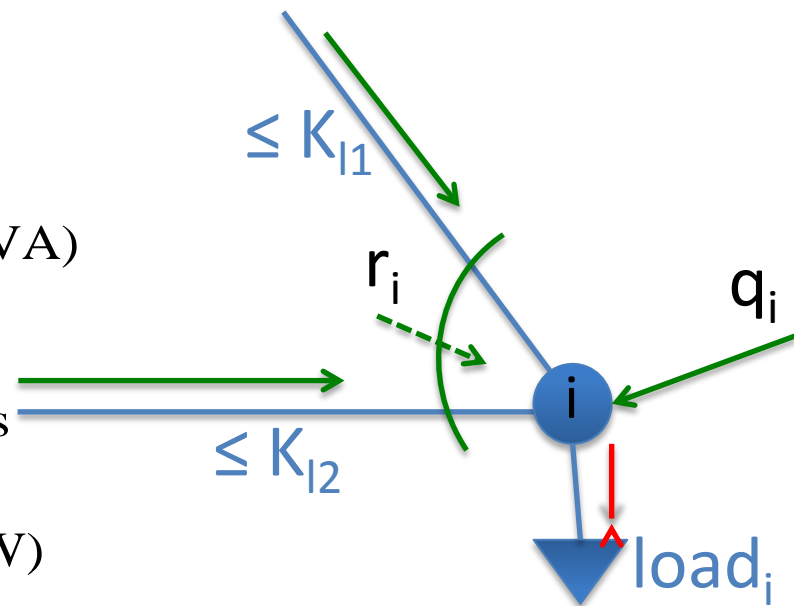
$\bar{q}_i$  Plant  $i$ 's maximum capacity (MW)

$$q_i + r_i = load_i, \quad \forall i \in N$$

$$\sum_{i \in N} r_i + Losses = 0$$

$$-K_l \leq \sum_{i \in N} D_{l,i} r_i \leq K_l, \quad \forall l \in L$$

$$\underline{q}_i \leq q_i \leq \bar{q}_i, \quad \forall i \in N$$



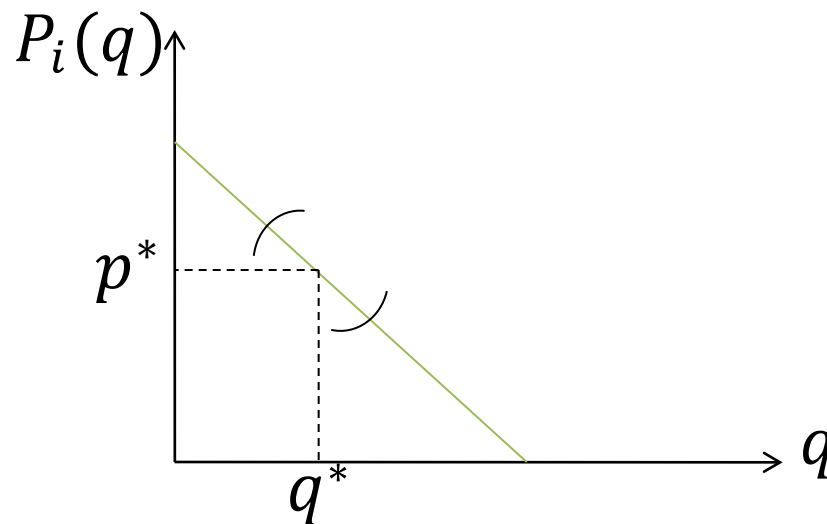


# Price-responsive demand

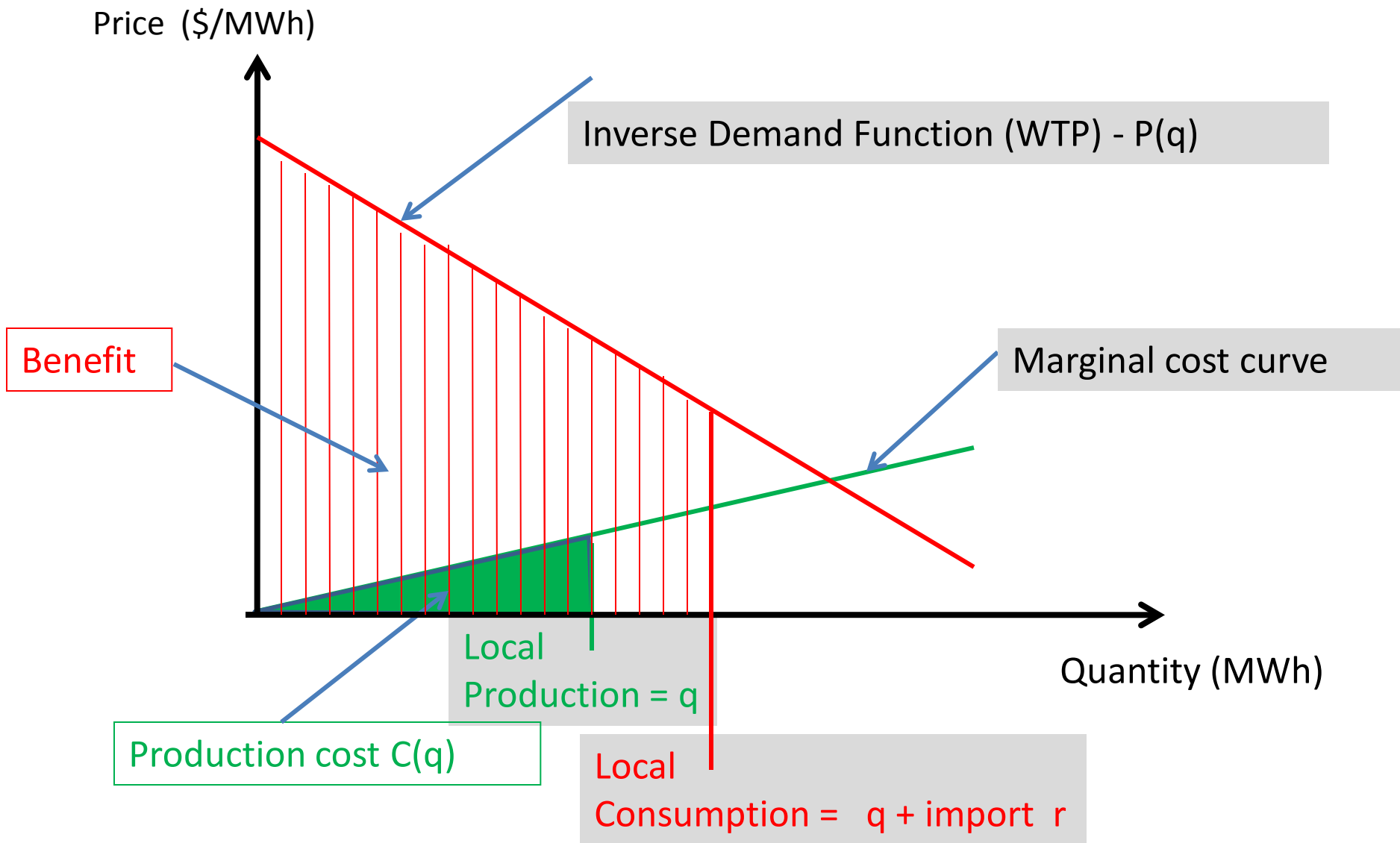
Consumers in each location  $i$  are represented by a linear inverse demand function:

$$P_i(q) = a_i - b_i q, \forall i \in N$$

- The inverse demand function at each bus is obtained from the results of a cost-minimizing power flow model.
- The price elasticity of demand is assumed to be -0.1 (Espey and Espey, 2004)



# ISO Maximizes Social Welfare subject to Transmission Constraints and Enforces CO2 Cap



# Equilibrium Model Mathematical Formulation (Linear Complementarity Problem)

ISO solves (redispatch problem)

$$\max_{r_i: i \in N} W = \sum_{i \in N} \int_0^{r_i + q_i} P_i(\tau_i) d\tau_i - C_i(q_i)$$

$$P_i(x) = a_i - b_i x, \forall i \in N$$

$$\text{s.t.} \quad \sum_{i \in N} r_i = 0 \quad (p)$$

$$\sum_{i \in N} D_{l,i} r_i \leq K_l, \forall l \in L \quad (\lambda_l^+)$$

$$-K_l \leq \sum_{i \in N} D_{l,i} r_i, \quad \forall l \in L \quad (\lambda_l^-)$$

KKT ISO:

$$P_i(q_i + r_i) = p + \varphi_i, \forall i \in N$$

$$\varphi_i = \sum_{l \in L} \lambda_l^+ D_{l,i} - \lambda_l^- D_{l,i}, \forall i \in N$$

$$\sum_{i \in N} r_i = 0$$

$$0 \leq \lambda_l^- \perp \sum_{i \in N} D_{l,i} r_i + K_l \geq 0, \quad \forall l \in L$$

$$0 \leq \lambda_l^+ \perp -\sum_{i \in N} D_{l,i} r_i + K_l \geq 0, \quad \forall l \in L$$

Each Firm  $g$  solves (profit maximization)

$$\max_{q_i: i \in N_g, p} \sum_{i \in N_g} (p + \varphi_i) q_i - C_i(q_i) - \mu e_i q_i$$

$$\text{s.t.} \quad \underline{q}_i \leq q_i \leq \bar{q}_i, \quad \forall i \in N_g$$

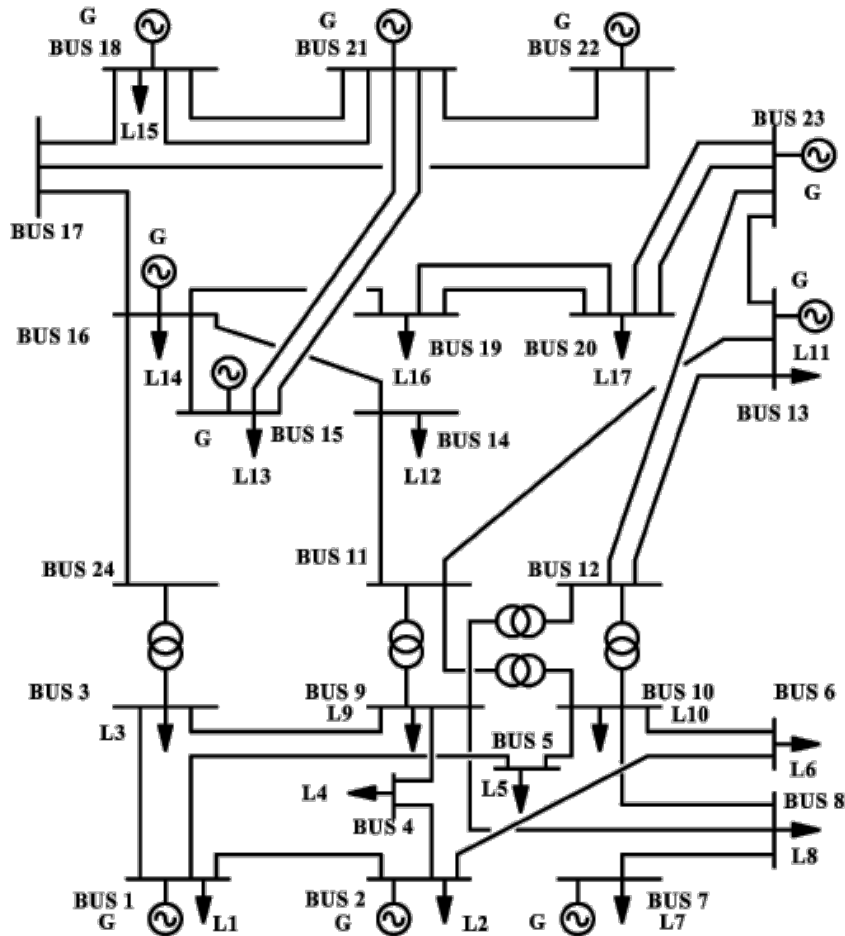
$$\sum_{i \in N} q_i = \sum_{i \in N} (P_i)^{-1} (p + \varphi_i)$$

CO<sub>2</sub> Market equilibrium

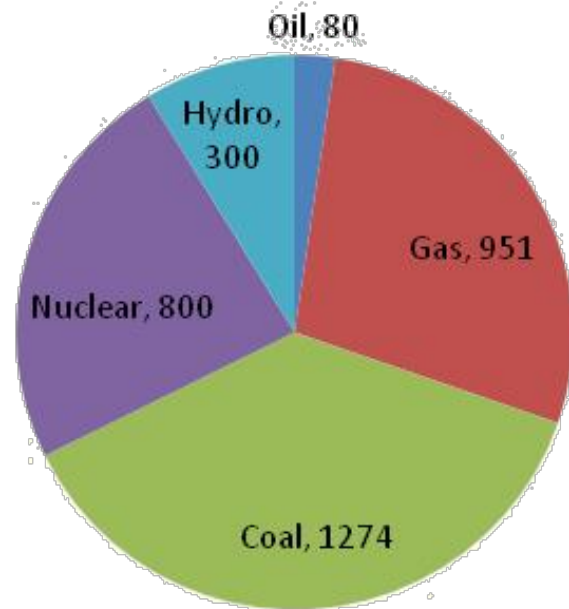
$$0 \leq \mu \perp M - \sum_{i \in N} F_i(q_i) \leq 0$$

$$F_i(q) = e_i q \quad \forall i \in N$$

# IEEE 24-Bus Test System – 3,405 MW Load



Fuel Type	\$/Mbtu	CO <sub>2</sub> (lbs/Mbtu)	# of units	Total MW
Oil	12	160	4	80
Gas	9.09	116	11	951
Coal	1.88	210	9	2174
Hydro	0	0	6	300
Nuclear	0	0	2	800



# IEEE 24 Bus: Market Scenario

Scenario	Description
PC	Perfect competition
N+H+24T	Oligopolistic competition with 26 firms in total: Nuclear firm, Hydro firm + 24 thermal firms
N+H+2T	Oligopolistic competition with 4 firms in total: Nuclear firm, Hydro firm +2 thermal firms
NH+G+CO	Oligopolistic competition with 3 firms in total: one firm owns all nuclear and hydro facilities, second firm owns all gas facilities, third firm owns all coal and oil facilities.
NHG+CO	Duopoly: one firm owns nuclear, hydro, and gas Second firm owns all coal and oil facilities.
MP	Monopoly: all facilities belong to only one firm.

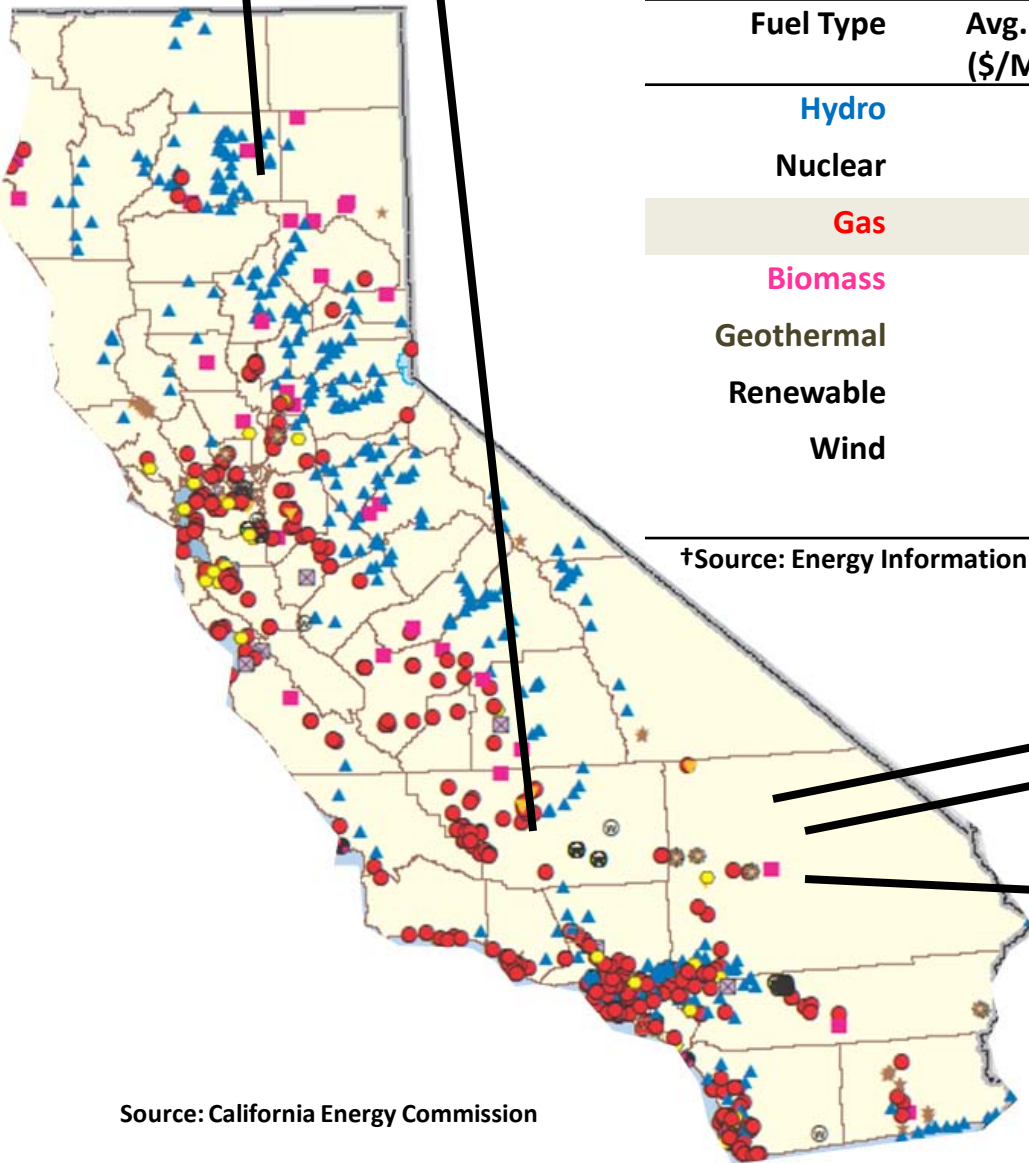
# IEEE 24 Bus: Electricity Price

## Ownership Structure

		PC	N+H+24	N+H+2	NH+G+CO	NHG+CO	MP	
CO <sub>2</sub> CAP	1205 Tons/h	Total CO <sub>2</sub> Emission [tons]	1,060	1,205	942	833	765	370
	Energy Consumption [MWh]	2,160	1,924	1,702	1,599	1,452	1,086	
	Avg. LMP [\$/MWh]	18	137	249	301	376	564	
	CO <sub>2</sub> Price [\$/ton]	0	66	0	0	0	0	
	CO <sub>2</sub> Emissions Rate [tons/MWh]	0.491	0.626	0.553	0.521	0.527	0.341	
	Congestion Rents [\$]	0	0	0	0	0	10,020	
	System Fuel Costs [\$]	38,750	67,401	36,379	62,991	32,834	24,906	
	515 Tons/h	Total CO <sub>2</sub> Emission [tons]	515	515	515	515	515	370
Energy Consumption [MWh]	1,734	1,556	1,537	1,367	1,294	1,086		
Avg. LMP [\$/MWh]	249	323	333	419	456	564		
CO <sub>2</sub> Price [\$/ton]	444	432	238	405	317	0		
CO <sub>2</sub> Emissions Rate [tons/MWh]	0.297	0.331	0.335	0.377	0.398	0.341		
Congestion Rents [\$]	170,959	0	0	0	0	10,020		
System Fuel Costs [\$]	66,649	63,629	56,158	49,113	27,877	24,906		

# Resource Mix

Imports



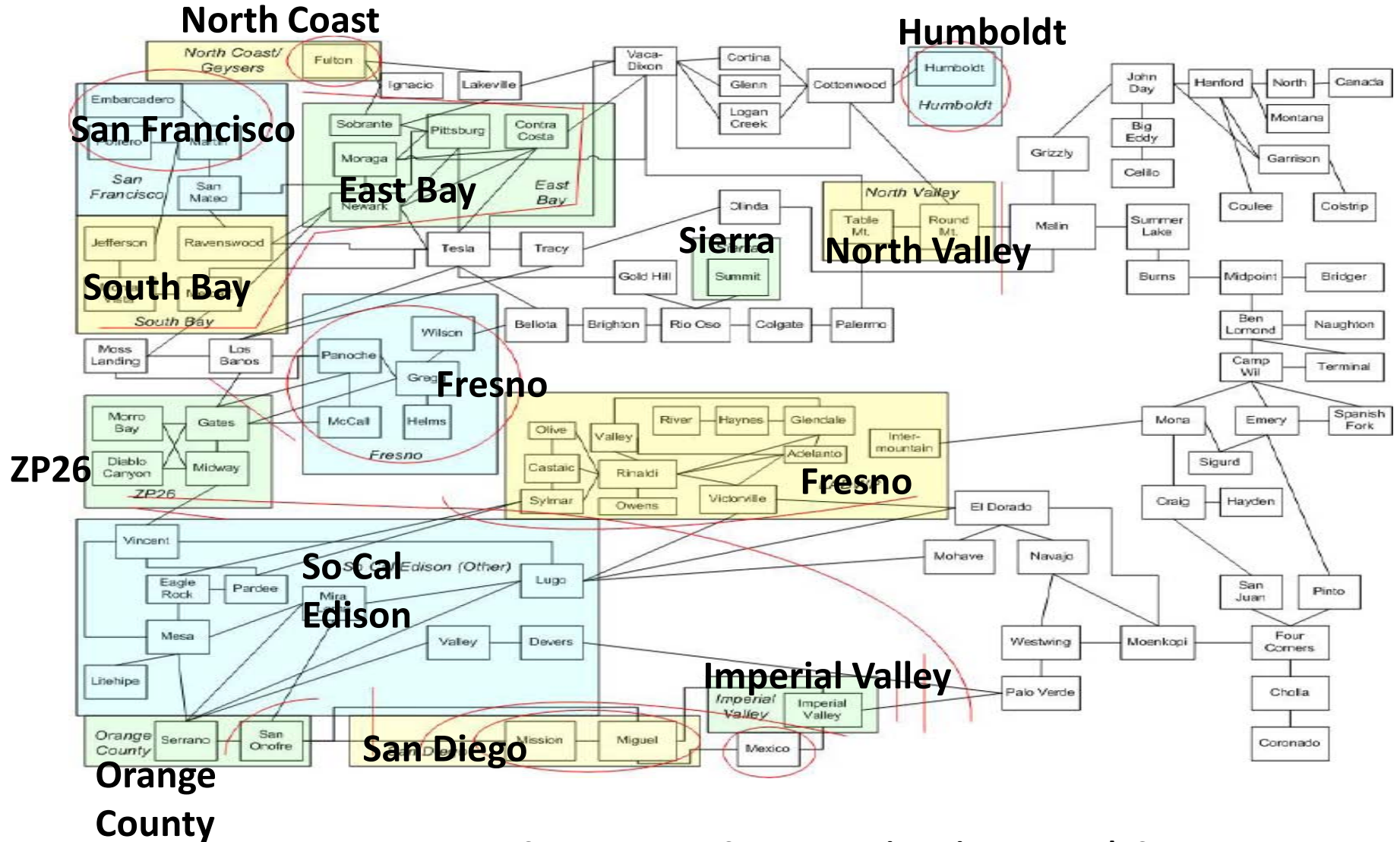
Fuel Type	Avg. MC† (\$/MWh)	Avg. CO <sub>2</sub> rate (lb/MWh)	Total MW	Percent
Hydro	7	0	10,842	23%
Nuclear	9	0	4,499	10%
Gas	70	1,281	26,979	57%
Biomass	25	0	558	1%
Geothermal	0	0	1,193	3%
Renewable	0	0	946	2%
Wind	0	0	2,256	5%
			<b>47,273</b>	<b>100%</b>

†Source: Energy Information Administration, Annual Energy Outlook 2010, DOE/EIA-0383(2009)

Import	Avg.CO <sub>2</sub> rate (lbs/MWh)
Arizona	1,219
Nevada	1,573
Oregon	456

Source: eGRID2006 V2.1, April 2007

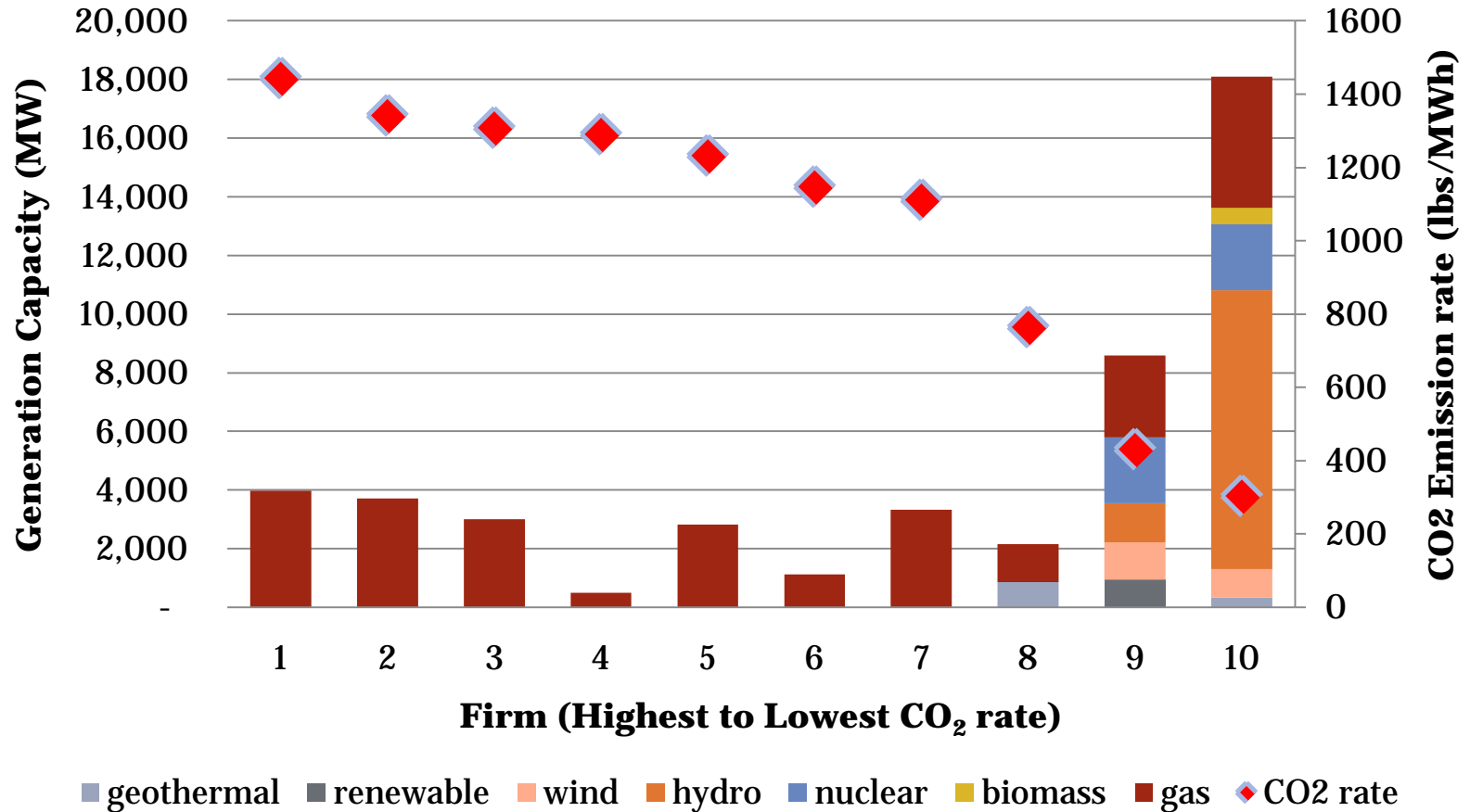
# WECC 225 Bus System





# Resource Mix by Firm

HHI Index by capacity = 2,100  
(Moderate Concentration)



# Test Case Scenarios and Assumptions

- Scenarios:

- Perfect Competition vs Oligopoly Competition
  - 10 firms with 1 competitive fringe
- No CO<sub>2</sub> cap and CO<sub>2</sub> cap (20% reduction below Perfect Competition with No Cap and Transmission Constraints)
- With/without transmission constraints

- Assumptions:

- Price-responsive linear demand function
  - with demand elasticity of -0.1 (Espey and Espey, 2004)
- Price-responsive linear supply function for imports
  - with supply elasticity of 0.005 (Tsao et. al., *Energy Policy* [2011])
- Simulated hour: the median load (Summer 2004)

# Economic Results 225 Bus Case (With/Without Tr. Constr.)

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	Perfect Competition				Oligopoly			
	No Cap		Cap		No Cap		Cap	
Total CO <sub>2</sub> Emission [tons]	6,111	4,977	4,889	4,889	9,766	9,611	4,889	4,889
Energy Consumption [MWh]	30,362	30,471	28,576	30,286	28,060	28,184	25,040	25,170
Avg. LMP [\$/MWh]	59	53	94	56	97	95	154	151
CO <sub>2</sub> Price [\$/ton]	0	0	74	8	0	0	155	151
CO <sub>2</sub> rate [ton/MWh]	0.201	0.163	0.171	0.161	0.348	0.341	0.195	0.194
Import CO <sub>2</sub> rate [ton/MWh]	0.465	0.464	0.465	0.464	0.464	0.464	0.464	0.464
In-State Fuel Costs (K\$)	347	235	245	225	663	651	215	216
Social Surplus (K\$)	10,386	10,511	10,348	10,510	9,899	9,923	9,968	9,988
Consumer Surplus (K\$)	8,945	9,135	7,905	9,033	7,839	7,906	6,320	6,400
Producer Surplus (K\$)	1,243	1,376	1,701	1,437	2,038	2,017	2,804	2,849
Congestion Revenues (K\$)	198	0	379	0	22	0	84	0

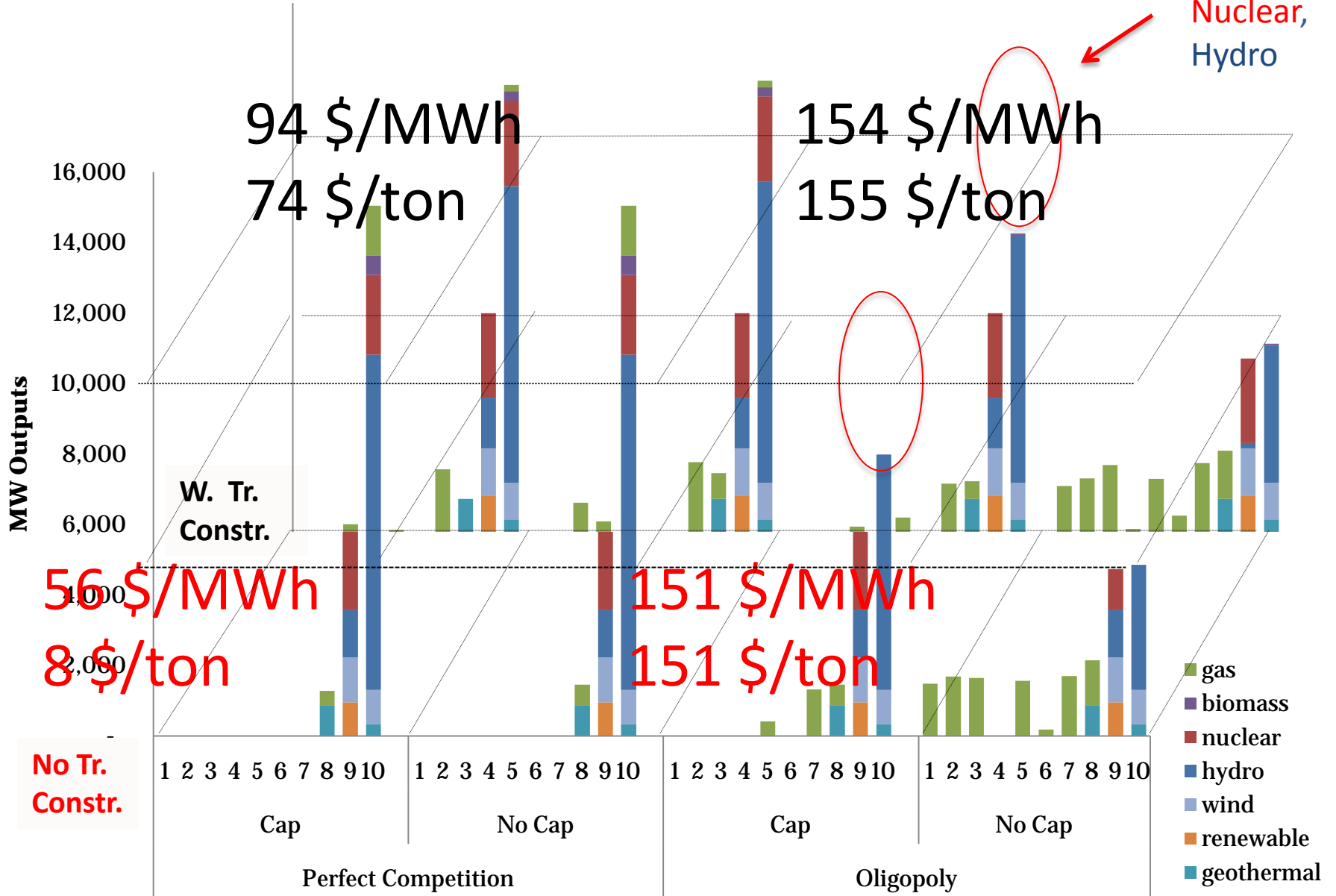
# Congestion VS No Congestion (With/Without Tr. Constr.)

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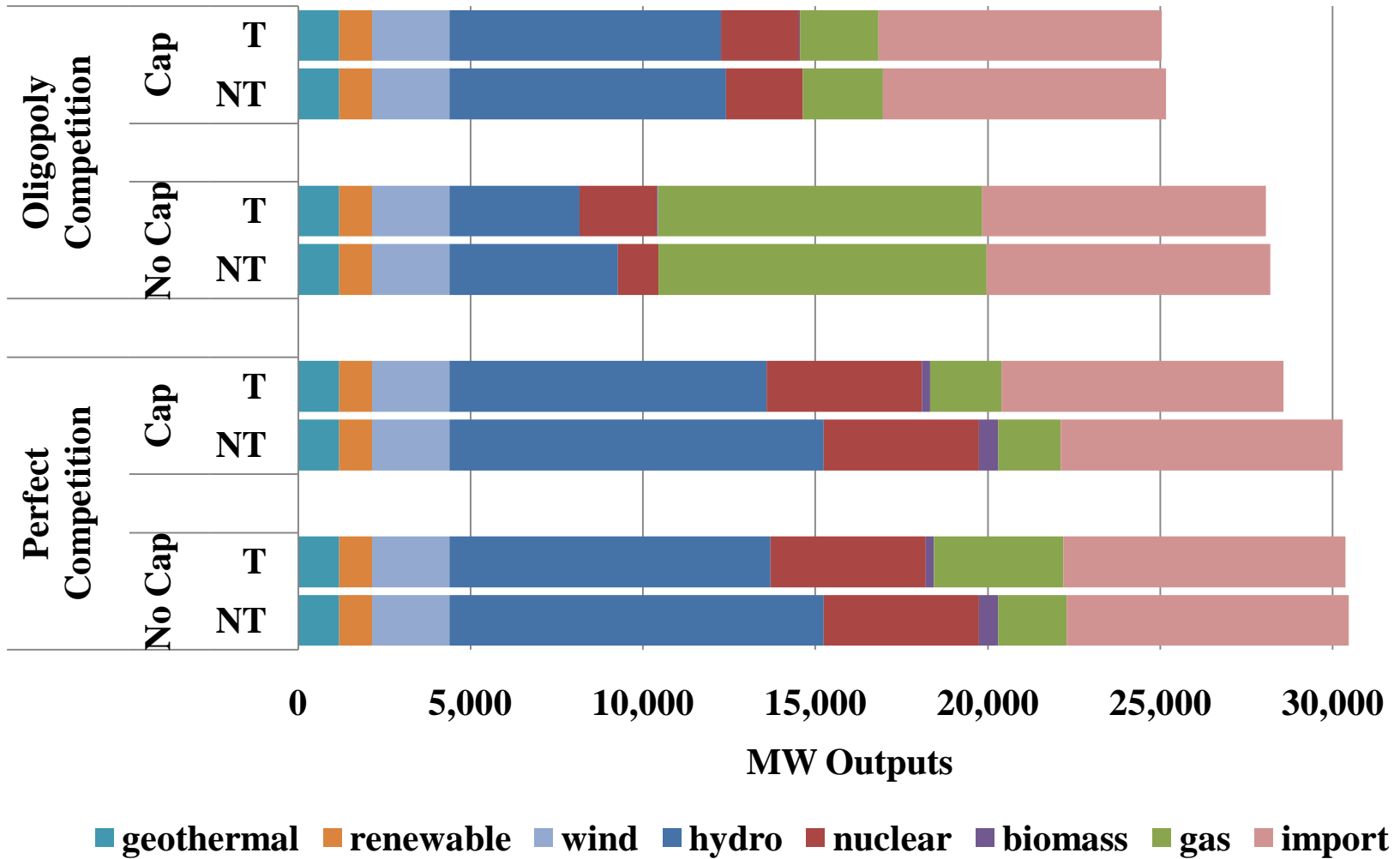
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# Equilibrium Results for Outputs by Firm

Gas,  
Biomass,  
Nuclear,  
Hydro



# Comparison of Equilibrium Outputs between Transmission-Constrained and Unconstrained Electricity Markets



# Implications of Simulation Studies

- We have demonstrated the need to consider the interaction of congestion and ownership structure (market power) in evaluating the impact of environmental policies on performance of the power system.
- Complex interaction may lead to unintended consequences that would not be revealed by simplified models.
  - A tight emission cap and ownership concentration of clean resources amplify market power effects.
  - In a transmission-constrained market, geographical concentration of clean resources can indirectly amplify market power via the permit market.
- Major Limitation of the Analysis:
  - One hour snapshot ignores intertemporal price smoothing in carbon market
  - Our carbon permit market targets only electricity and ignores the impact of other industry sectors participating in C&T on permit prices.

# Questions?

