

Do costs fall faster than revenues? Renewable Electricity Subsidies' Dynamics

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- Subsidies to renewable generation can be justified by learning-by-doing externalities
 - Costs will fall over time
- The value of the output from renewable generators depends on the mix of plant on the system
 - Too much of a good thing falls in value
- Which of these effects will dominate in practice?





- We present:
 - 1. the basic story
 - 2. a theoretical model
 - 3. a numerical simulation
- We find:
 - 1. For numbers fitted to wind energy in Great Britain, the falling price effect appears to dominate so subsidies are "always" required (for our fuel and carbon prices)
 - 2. Low learning rates lead to large welfare losses
 - Marginal loss is £100 per kW per year at 30 GW
 - Cumulative loss of £2 billion per year





















































The model



- Renewable capacity marginal cost r₀(K₀) falls with learning by doing, cumulative cost R₀(K₀)
- Renewables are paid a feed-in tariff to cover their cost

 $f(K_{0}) \mathbb{E} \left[\alpha \left(\theta \right) \right] = r_{0} \left(K_{0} \right)$

where α is renewable availability in state θ

 First units require a subsidy φ(K₀) (in € per MW of capacity per hour) as their cost exceeds expected revenue at market prices

 $\varphi(K_{0}) = \max(r_{0}(K_{0}) - \mathbb{E}[\alpha(\theta)p(\theta, K_{0})], 0)$

• Subsidy is financed via a tax, τ , paid by consumers



• No change in (time-weighted) average price, $p(\theta, K_0)$

$$\mathbb{E}\left[\frac{\partial p}{\partial K_0}\left(\theta, K_0\right)\right] = 0$$

• Reduction in conventional installed capacity

$$\frac{dK_{n}}{dK_{0}} = -\frac{1}{b}\frac{d\tau}{dK_{0}} - \mathbb{E}\left[\alpha\left(\theta\right)|v_{n}\right]$$

- K_n is cumulative capacity of first *n* types (ordered by MC)
- *b* is demand curve slope



• (Expected) Tax revenues cover cumulative capital cost of renewable generation, $R_0(K_0)$ $R_0(K_0) = \tau \overline{D}(K_0) + \mathbb{E}[p(\theta, K_0) \alpha(\theta) K_0]$

where expected demand is

 $\bar{D}(K_{0}) = \mathbb{E}\left[D\left(p\left(K_{0}, \theta\right) + \tau\left(K_{0}\right), \theta\right)\right]$

• Full differentiation leads to

$$\frac{d\tau}{dK_0} \overline{D}(K_0) = \varphi(K_0) - \tau \frac{d\overline{D}}{dK_0} - \mathbb{E} \left[a(\theta) \frac{\partial p}{\partial K_0} \right] K_0$$

the E/MW per hour subsidy for change in market revenues incremental capacity K_0

Exploiting the Imperial College structure of the supply **BUSINESS SCHOOL** curve (linear demand)



Marginal demand reduction lacksquare

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$$\frac{d\bar{D}}{dK_0} = -\frac{1}{b}\frac{d\tau}{dK_0}$$

Marginal revenues reduction for renewables \bullet

$$\mathbb{E}\left[\alpha\left(\theta\right)\frac{\partial p}{\partial K_{0}}\right] = -b\widehat{var}_{K_{0}}\left[\alpha\left(\theta\right)\right]$$

Conditional variance of α on the vertical parts of the supply curve

Marginal tax increase lacksquare

$$\frac{d\tau}{dK_{0}} = \frac{b\left(\varphi\left(K_{0}\right) + bK_{0}\widehat{var}_{K_{0}}\left[\alpha\left(\theta\right)\right]\right)}{b\bar{D}\left(0\right) - 2\tau\left(K_{0}\right)}$$



• Marginal subsidy

$$\varphi\left(K_{0}\right)=r_{0}\left(K_{0}\right)-\mathbb{E}\left[p\left(\theta,0\right)\alpha\left(\theta\right)\right]+b\int_{0}^{K_{0}}\widehat{var}_{x}\left[\alpha\left(\theta\right)\right]dx$$

• Marginal welfare change

$$\frac{dH}{dK_0} = -\varphi\left(K_0\right) + \tau \frac{d\bar{D}}{dK_0}$$

$$\frac{dH}{dK_{0}} = -\left(\frac{\left(b\bar{D}\left(0\right) - \tau\left(K_{0}\right)\right)\varphi\left(K_{0}\right) + \tau\left(K_{0}\right)\widehat{var}_{K_{0}}\left[\alpha\left(\theta\right)\right]bK_{0}}{b\bar{D}\left(0\right) - 2\tau\left(K_{0}\right)}\right)$$



• Marginal subsidy

$$\varphi(K_{0}) = r_{0}(K_{0}) - \mathbb{E}\left[p(\theta, 0) \alpha(\theta)\right] + bK_{0}\widehat{var}\left[\alpha(\theta)\right]$$

• Marginal welfare change

$$\frac{dH}{dK_{0}} = -\left(\frac{\left(b\bar{D}\left(0\right) + \sqrt{\Delta\left(K_{0}\right)}\right)\varphi\left(K_{0}\right) + \left(b\bar{D}\left(0\right) - \sqrt{\Delta\left(K_{0}\right)}\right)\widehat{var}_{K_{0}}\left[\alpha\left(\theta\right)\right]bK_{0}}{2\sqrt{\Delta\left(K_{0}\right)}}\right)$$



• Marginal subsidy

$$\varphi(K_{0}) = r_{0}(K_{0}) - \mathbb{E}\left[p(\theta, 0) \alpha(\theta)\right] + bK_{0}\widehat{var}\left[\alpha(\theta)\right]$$

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where
$$\Delta(K_0) = (b\bar{D}(0))^2 - 4b\Phi(K_0)$$

and $\Phi(K_0) = R_0(K_0) + K_0(\widehat{var}[\alpha(\theta)]bK_0 - \mathbb{E}[p(\theta, 0)\alpha(\theta)])$.



• Capital cost of renewable (composite onshore and offshore wind) capacity with learning rate β

$$r_{0}\left(K_{0}\right) = \frac{320000}{8760} \times \left(\frac{10000}{K_{0}}\right)^{\beta}$$

- We study three learning rates, with a cost decrease of 10%, 19% or 30% each time capacity doubles
- Plant costs for nuclear, CCGT and OCGT taken from DECC (2013) study of generation costs, including predicted future carbon taxes rising to £70/tonne
- Demand and load factor data from Green and Staffell (2013)



Imperial College London BUSINESS SCHOOL MARGINAL SURPLUS IOSS Sometimes increasing









- Learning by doing should reduce feed-in tariffs as more renewable energy is installed
- The value of renewable energy falls as more is produced
- With our calibration, the second effect dominates, hence subsidies are always required
 - We measure subsidy by the difference between the FiT and the value of the energy produced
- Further work will examine the incentives created by different support mechanisms and levels of priority dispatch
- We also examine the cost of additional operating reserves required to manage renewable intermittency





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variance approximationToulouse
SchoolBUSINESS SCHOOLVariance approximationof Economics





