

# Patents in a Model of Growth with Persistent Leadership

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- In many sectors: cumulative quality improving/ cost reducing innovation
- Unlike in most quality-ladder models, industry leaders often do a lot of R&D:

Bartelsman and Doms (2000) and Foster, Haltiwanger and Krizan (2001): net entry accounts for about one fourth of productivity growth in the US manufacturing sector; about half of it was due to within plant growth

Other studies: Malerba and Orsenigo (1999); Czarnitzky, Etro and Kraft (2009)...

- I analyze the effect of different patent policies within the context of a quality-ladder growth model in which there is persistent leadership

- O' Donoghue and Zweimüller (2004) and Hopenhayn, Llobet and Mitchell (2006): leapfrogging case
- Bessen and Maskin (2009) and Acemoglu and Akcigit (2009): duopoly case
- Denicolò and Zanchettin (2010); assume that leader is better in doing R&D

Main difference in my model:

- 1 all technologies are nonrival and access to them is only restricted by IP
- 2 possibility of preemption

# The Model Setup

- There is a good the quality of which can be increases step-by-step through innovation
- Flow profits of a firm producing the newest version of the good depend on whether the firm has a patent (preventing imitation of this version of the good) and on how far it is ahead of its rivals
- Without patent protection: Bertrand competition  $\pi_0 = 0$
- One-step lead: limit pricing  $\pi_1$
- Two- or more-step lead:  $\pi_2$ , with  $\pi_2 > \pi_1 > 0$

Profit flows are for simplicity assumed to be independent of quality level (but looked at more general case as well)

- R&D technology: the instantaneous arrival rate  $\phi$  of an innovation can be obtained at the total (industry) costs

$$C(\phi) = \begin{cases} c\phi^{1+\varepsilon} & \text{if } \phi \leq \phi_m \\ \infty & \text{if } \phi > \phi_m \end{cases}$$

- Marginal R&D costs increase at the industry level (due to duplication or an upward sloping supply curve for R&D inputs)
- If more than one firm does R&D, its innovation probability is given by  $\alpha\phi dt$  if its share in total R&D costs is given by  $\alpha$

In order to simplify calculations later on, an upper bound  $\phi_m$  on the total arrival rate is assumed and the case where  $\varepsilon \rightarrow 0$  is analyzed.

- Time is continuous and the rate of interest is exogenous and given by  $r$
- In the basic setup, patents are infinitely lived but effective patent length depends on the probability of being replaced by a new innovator
- Free entry into the R&D sector: an entrant without patent must get zero expected profits
- In equilibrium, the value of an innovation for an entrant cannot exceed the average cost of undertaking R&D:

zero profit condition

$$V_E \leq c\phi^\varepsilon$$

- An incumbent with a two-step lead in an industry has no stand-alone incentives to do R&D. However, the ZP - condition pins down an innovation rate which is independent of whether the incumbent herself innovates or not
- As the incumbent values not being replaced more than entrants value entry (as  $\pi_2 > \pi_1$ ), she wants to preempt entry. If the incumbent moves first in the R&D game, she does all the R&D necessary to satisfy the zero profit condition so that there is no entry in equilibrium (look at MPE)
- Persistent leadership!
- Same reasoning as in Gilbert and Newbery (1982) and Denicolò (2001)

The value of an innovation for an entrant expecting to become the next incumbent is given by:

## Value of an innovation

$$V_E = \frac{\pi_1 - c\phi_1}{r + \phi_1} + \frac{\phi_1}{r + \phi_1} \frac{\pi_2 - c\phi_2}{r} \text{ where either } \phi_1 = \phi_2 \text{ or } \phi_1 = \phi_m > \phi_2$$

- If the incumbent has a two-step lead, the zero profit condition  $V_E = c$  determines the equilibrium innovation rate as a positive function of profit flows and a negative function of  $c$  and of  $r$ .
- Policies that increase  $V_E$  lead to an increased rate of innovation!

- VOLUNTARY DEALS: If incumbents cannot commit to compete, allowing them to consolidate market power with entrants (which increases  $\pi_1$ ) and to coordinate joint R&D spendings (which can lead to cost reductions in the case where  $\phi_1 = \phi_m$ ) increases entry pressure and growth (similar to Segal and Whinston (2007))
- R&D incentives are maximal if entrant gets  $\pi_2$  directly if enters

Implementable through a “PATENT TRANSFER SCHEME”: force incumbent to freely give all patents to entrant if innovation occurs  
→ also works in the case of leapfrogging and in product variety settings

- Compensating previous innovators by requiring entrants to pay a fee  $F$  to the previous incumbent upon replacement

zero profit condition:  $V_E = c + F$

→ reduces growth

- LEADING BREADTH (of one step): the innovation of an entrant infringes on the patent of the incumbent

Assumption: without forward protection, no voluntary deals

→ decreases growth, unless it allows for considerable reductions in R&D costs

- Different in the case of leapfrogging! (O'Donoghue/Zweimüller 2004)

## Variable Innovation Size $\mu$

$$C_i(\phi_i, u_i) = c\lambda(\mu_i)\phi_i (C_{tot})^\varepsilon \text{ with } \frac{\partial \lambda}{\partial \mu} > 0 \text{ and } \pi_1 = \pi_1(\mu)$$

- Restricting the choice of the inventive step reduces entry pressure and therefore the amount that incumbents need to spend on R&D in order to preempt entry
- Imposing a patentability requirement only on the incumbent might however be useful to avoid inefficiently small inventive steps (need to be able to distinguish between incumbents and entrants...)
- Different in the case of leapfrogging, where a patentability requirement can prevent low markups, an excessive rate of turnover and inefficiently small inventive steps.

# Varying Enforcement Probability

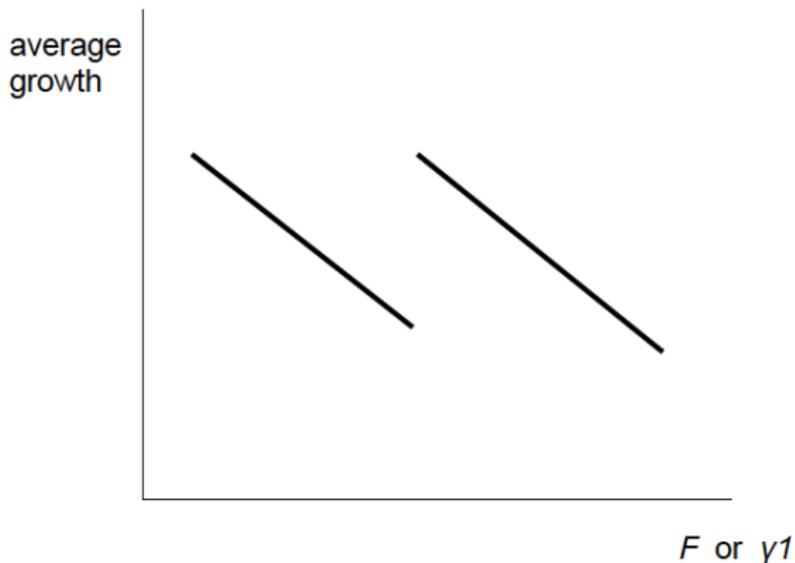
- Patents expire with probability  $\gamma_1$  ( $\gamma_2$ ) if one (two) steps ahead (“STATE DEPENDENT IPR” like in Acemoglu and Akcigit (2009))

$$V_E = \frac{\pi_1 - c\phi_1}{r + \gamma_1 + \phi_1} + \frac{\phi_1}{r + \gamma_1 + \phi_1} \frac{\pi_2 - c\phi_2}{r + \gamma_2}$$

- If  $\gamma_1$  is similar to  $\gamma_2$ , we have  $\phi_1 = \phi_2$  and increasing the probabilities of expiration reduces the value of an innovation for an entrant and growth.
- However, if  $\gamma_1$  is large enough relative to  $\gamma_2$  or if there are large enough fixed costs of entry ( $F$ ) we get:

$$\frac{\partial V_E}{\partial \phi_1} > 0 \text{ so that } \phi_1 = \phi_m > \phi_2$$

Then, the R&D incentives are higher in industries with a one-step lead compared to industries with a two-step lead or industries where firms are neck-and-neck



- In the case where  $\phi_1 = \phi_m > \phi_2$ , increasing  $\gamma_2$  can increase the share of industries in which the leading firm is one step ahead. However, it also leads to a decrease in  $\phi_2$  and this effect is stronger than the composition effect, so that average growth decreases.

# Possible Perils of Strong Patents

Under full patent protection, incumbents might be able to preempt entry without doing R&D themselves if:

- 1 Entrants have to pay a fixed (catch-up) cost in order to enter the R&D sector and incumbents can readjust their R&D effort after observing entry
  - 2 Incumbents can hire the most able researchers but make them do other things than R&D instead
  - 3 Incumbents can make ex ante agreements with potential entrants to reduce R&D effort
- In these cases, equilibrium growth is zero under full patent protection
  - An intermediate probability of patent enforcement (finite patent length) maximizes average growth (similar to Horowitz and Lai (1996)). Reducing patent breadth/ markups does not have the same effects

- In order to improve the quality of the good by one step, two R&D stages have to be completed. Again, preemption is possible at each stage.
- Growth is maximal if entrants are allowed to patent intermediate R&D inputs (but not allowed to license them to incumbents) but incumbents are not
- Incumbents still race to invent the intermediate R&D inputs in order to prevent that an entrant patents them. At the second R&D stage, the analysis is the same as above...

- While the current literature focuses on the case of leapfrogging, I analyze the other extreme of persistent leadership
- While R&D incentives are increased in both cases if entrants get considerable market power right upon entry, the effects of leading breadth and of a patentability requirement are different.
- Making patent policy conditional on whether an entrant or an incumbent innovates can stimulate innovation and growth.
- In some cases, an intermediate strength of patent protection maximizes average growth
- The main results are the same if a more general model with increasing profit flows is analyzed
- Restrictions: continuous quality-ladder without initial innovator (different in Chu, Cozzi and Galli (2010)); perfect preemption

# Increasing Profit Flows

- Utility is given by:  $U(\tau) = \int_{t=\tau}^{\infty} c(t)e^{-\rho(t-\tau)} dt$
- Final good  $y$  which can be consumed, used for research or to produce intermediate goods  $x$  of which there exist different generations (the newest one indexed by  $k$ )
- The final good is produced using labour (in fixed supply) and intermediate goods according to the following production function

$$y(k) = X_k^\alpha \text{ with } X_k = \sum_{s=0}^k q^s x_s \text{ and } 0 < \alpha < 1$$

- Only the newest generation of intermediate goods is in use:  
 $y(k) = q^{k\alpha} x_k^\alpha$

- Deriving the demand for the newest intermediate good and assuming that  $\alpha q \leq 1 \leq \alpha q^2$ , patent holders with a two-step lead charge the unconstrained monopoly price while those with a one-step lead engage in limit pricing
- Profits for generation  $k$  of the good are given by

$\pi_1(k) = \pi_1 g^k$  and  $\pi_2(k) = \pi_2 g^k$ . The Arrow replacement effect is present

- R&D sector:  $\phi(k+1) = \min \left\{ \left( \frac{n}{cg^k} \right)^{\frac{1}{1+\varepsilon}} ; \phi_m \right\}$
- Qualitatively, the main results are the same