



# **Optimal Transmission Switching: When Economic Efficiency and FTR Markets Collide**

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# Overview

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- Motivation for transmission switching
  - Economic efficiency through topology improvements with no reliability degradation
  - Smart grid application by exploiting short term network reconfiguration flexibility
  
- Analyze market implications of optimal transmission switching
  - May undermine prevailing market mechanisms – cause revenue inadequacy in the FTR market
  - Unpredictable distributional impacts on LMPs, generation rent, congestion rent, etc.

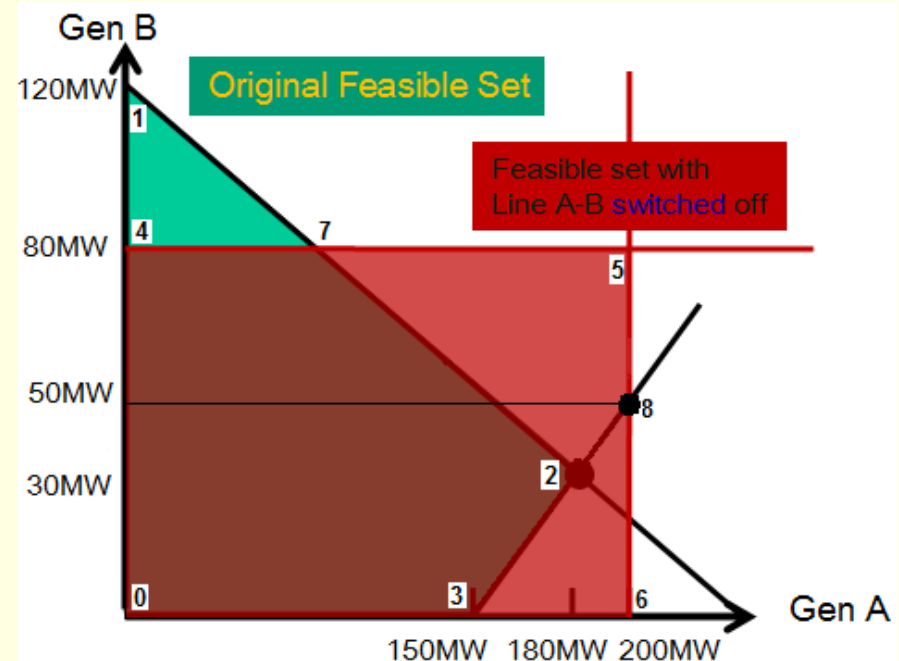
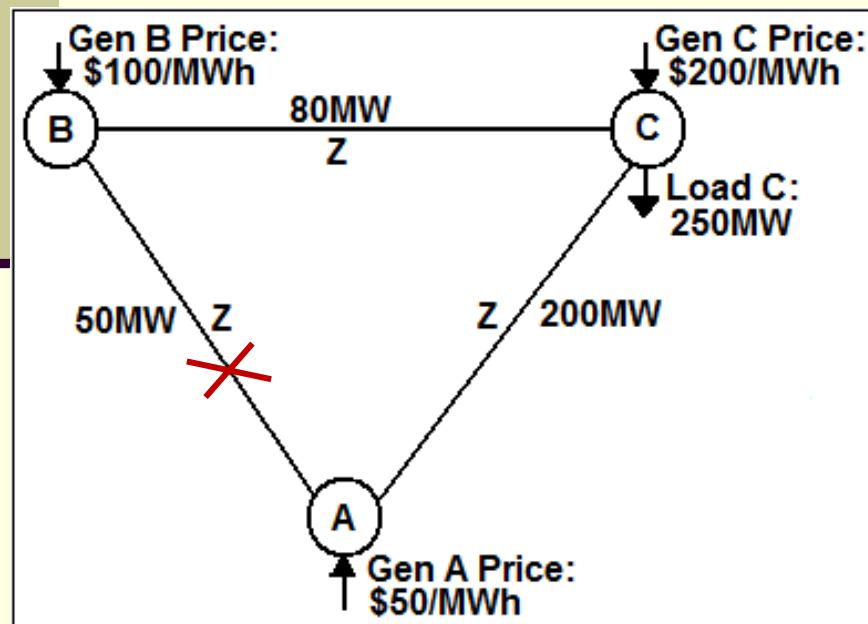
# Overview of Optimal Transmission Switching Concept

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- Control of transmission not fully utilized today
  - Transmission assets are seen as static in the short term
  - Currently operators change transmission assets' states on ad-hoc basis (per private communication with Andy Ott, VP, PJM)
- Network redundancies
  - Required for reliability, not required for every market realization
  - Redundancies may cause dispatch inefficiency
- Optimal transmission switching: co-optimize network topology with generation dispatch

# Transmission Switching Example

- Original optimal cost: \$20,000 (A=180MW, B=30MW, C=40MW) at {2}
  - Original feasible set: {0,1,2,3}
- Open Line A-B, optimal cost: \$15,000 (A=200MW, B=50MW) at {8}
  - Feasible set with Line A-B open {0, 4, 5, 6}
- Feasible set with optimal transmission switching: {0, 1, 7, 5, 6} (non-convex)



# Literature Review

## Corrective switching

- *[Mazi, Wollenberg, Hesse 1986]: Corrective control of power systems flows*
- *[Schnyder, Glavitsch 1990]: Security enhancement using an optimal switching power flow*
- *[Glavitsch 1993]: Power system security enhanced by post-contingency switching and rescheduling*
- *[Shao, Vittal 2006]: Corrective switching algorithm for relieving overloads and voltage violations*

## Switching to reduce losses

- *[Bacher, Glavitsch 1988]: Loss reduction by network switching*
- *[Fliscounakis, Zaoui, et al. 2007]: Topology influence on loss reduction as a mixed integer linear program*

## Switching to relieve congestion

- *[Granelli, Montagna, et al. 2006]: Optimal network reconfiguration for congestion management by deterministic and genetic algorithms*

# Traditional DCOPF

- Minimize: Total generation cost

Subject to:

- Generator min & max operating constraints
- Node balance constraints
- Line flow constraints

$$B_k (\theta_n - \theta_m) - P_k = 0$$

- Line capacity constraint

- **Variables:**

$P_k$ : real power flow from bus  $m$  to bus  $n$  for line  $k$

$P_g$ : Gen  $g$  supply at bus  $n$

$\theta_n$ : Bus  $n$  voltage angle

$z_k$ : Transmission line status (1 closed/in service, 0 open/out of service)

- **Parameters:**

$B_k$ : Susceptance of line  $k$

$d_n$ : Real power load at bus  $n$

# Incorporating Transmission Switching into DCOPF

- $z_k$ : State of transmission line (Binary: 0 open/offline, 1 closed/operational)

- Update line thermal (capacity) constraints:

- Original:  $P_k^{\min} \leq P_k \leq P_k^{\max}$

- New:  $P_k^{\min} z_k \leq P_k \leq P_k^{\max} z_k$

- Update line flow constraints:

- Original:  $B_k (\theta_n - \theta_m) - P_k = 0$

- New:  $B_k (\theta_n - \theta_m) - P_k + (1 - z_k) M_k \geq 0$   
 $B_k (\theta_n - \theta_m) - P_k - (1 - z_k) M_k \leq 0$

# Optimal Transmission Switching DCOPF

$$\text{Minimize: } \sum_g (c_g P_g)$$

*s.t.*

Node Balance Constraints:

$$\sum_{\forall k(n,.)} P_k - \sum_{\forall k(.n)} P_k + \sum_{\forall g(n)} P_g = d_n, \forall n$$

Generator Constraints:

$$0 \leq P_g \leq P_g^{\max}, \forall g$$

Transmission Constraints:

$$P_k^{\min} z_k \leq P_k \leq P_k^{\max} z_k, \forall k$$

$$B_k(\theta_n - \theta_m) - P_k + (1 - z_k)M_k \geq 0, \forall k$$

$$B_k(\theta_n - \theta_m) - P_k - (1 - z_k)M_k \leq 0, \forall k$$

$$z_k \in \{0,1\}.$$

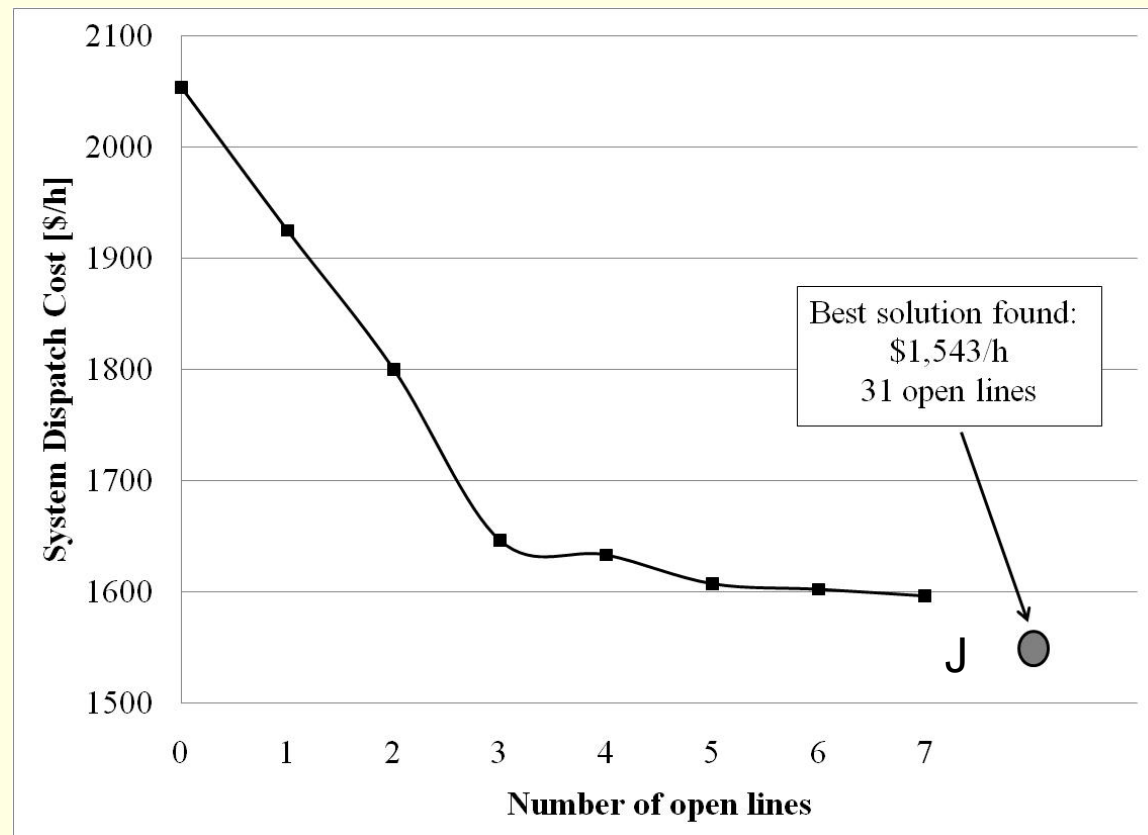


# Economic Savings for DCOPF and N-1 DCOPF Models

- DCOPF Transmission Switching Model (one hour):
  - IEEE 118 Bus Model: saves **25%** saving (10 lines off)
  - ISONE 5000 Bus Model: **5%-13% savings (\$70,000 savings)**
  - With advanced smart grid technology, switch lines back into service for a contingency to meet N-1 (just-in-time transmission)
- N-1 DCOPF Transmission Switching Model (one hour):
  - IEEE 73-Bus Model: **up to 8% savings**
  - IEEE 118-Bus Model: **up to 16% savings**
  - Ensures N-1 within transmission switching model
  - Improves efficiency of grid while ensuring N-1 Reliability<sup>9</sup>

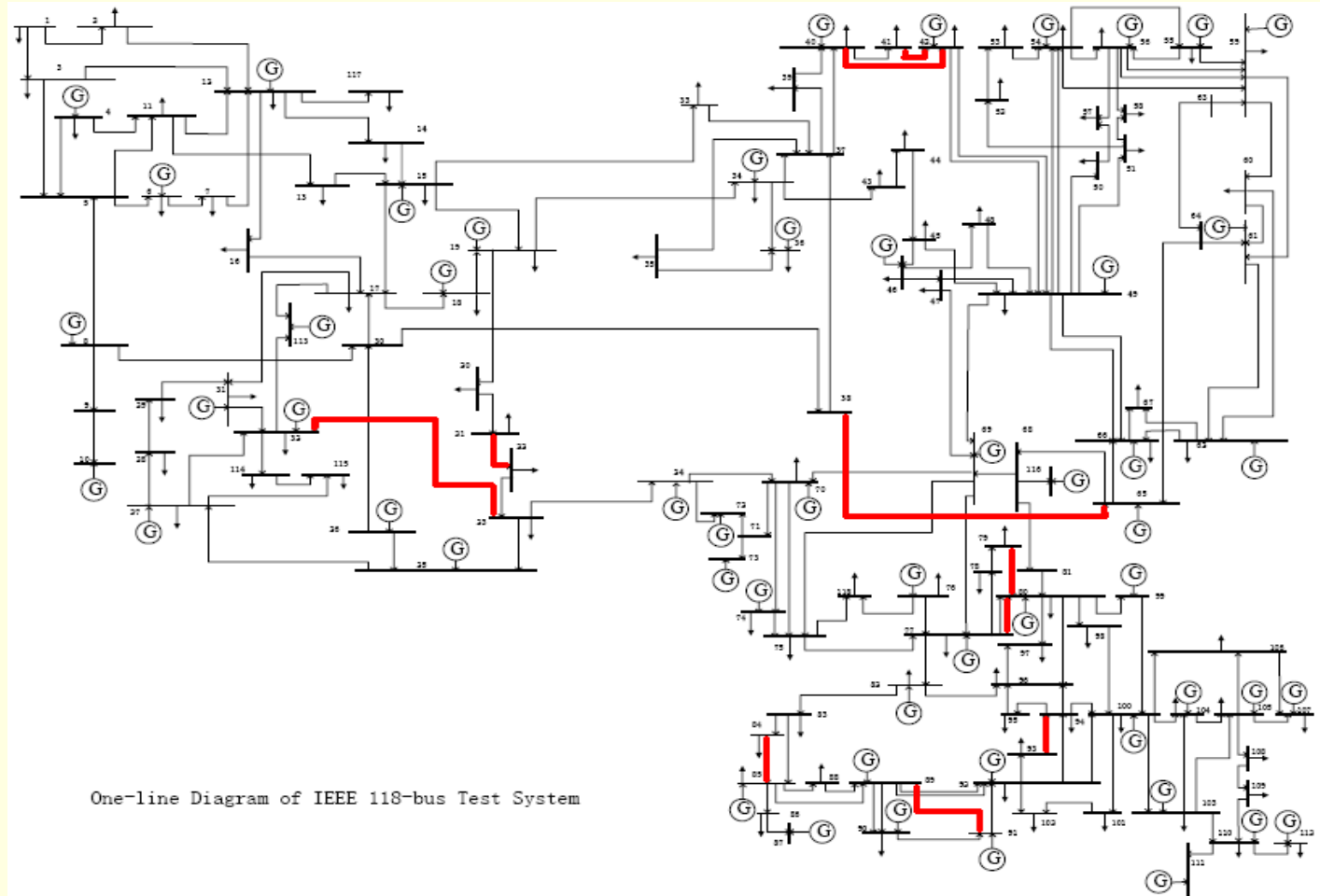
# Results – DCOPF – IEEE 118

- Transmission switching solution saves 25% of total generation cost



# Results – DCOPF – IEEE 118

- IEEE 118  
opened  
lines for  
 $J=10$
- Note: this  
diagram  
has  
additional  
gens than  
our model



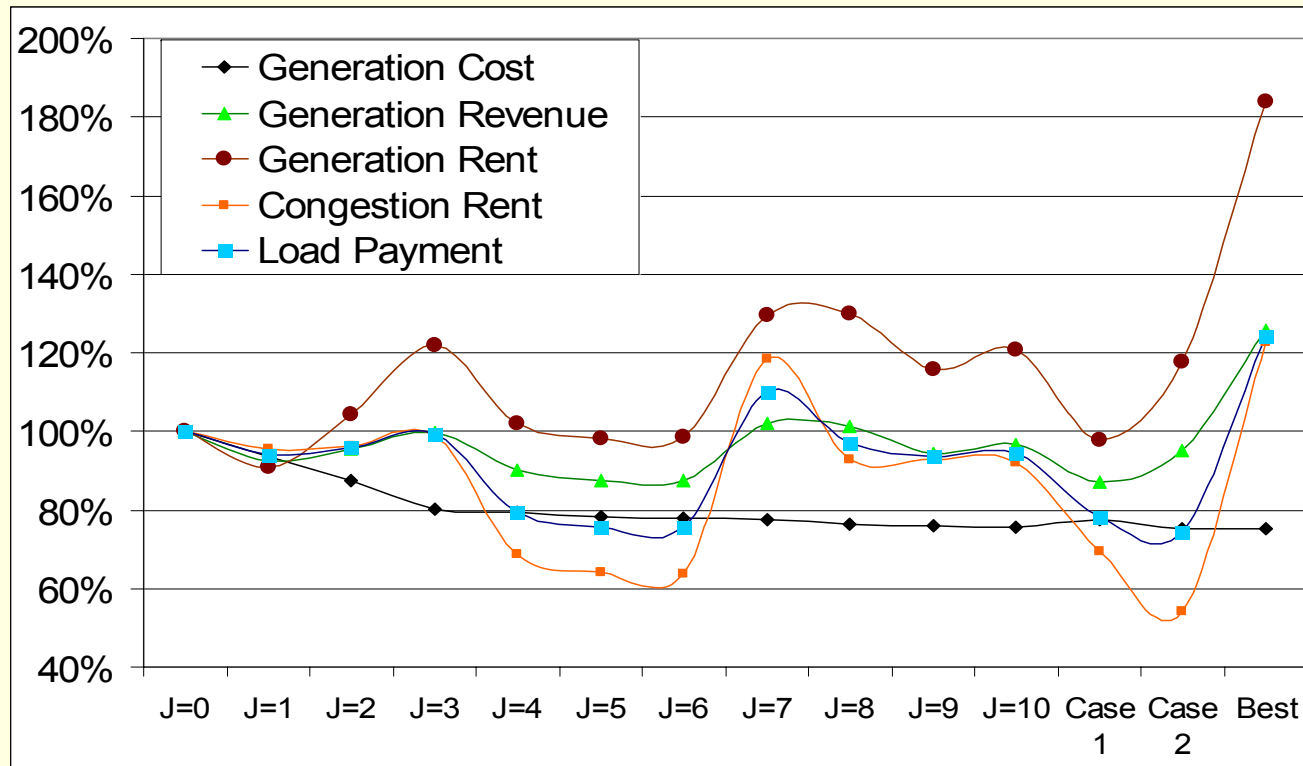
# Economic Savings for UC with Transmission Switching

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- Generation Unit Commitment N-1 DCOPF Transmission Switching Model:
  - IEEE 73-Bus Model: **3.7% savings (\$120,000 savings for 24-hour model)**
  - Unit commitment solution changes when topology changes
  - Peaker units committed with original topology - not committed under co-optimization of network topology and unit commitment
  - Optimal topology varies hour to hour

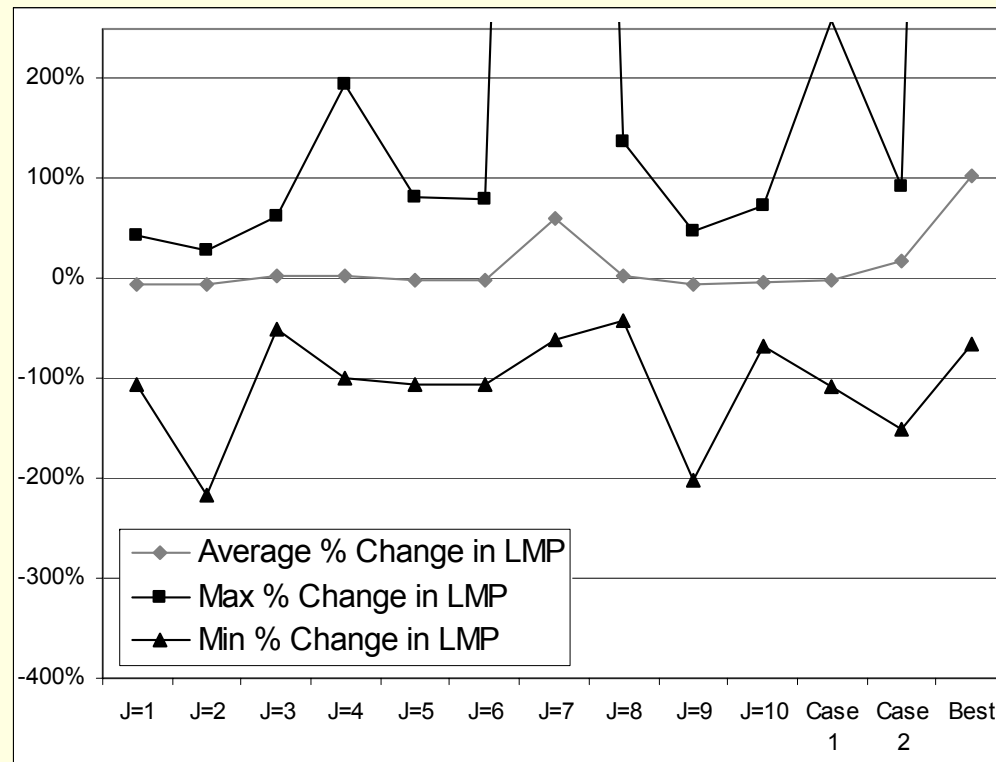
# Impact on Market Participants

- Results are % of static network's DCOPF solution
- Unpredictable distributional effects for market participants



# Impact on LMPs

- Max and min percent change in LMP
  - IEEE 118 bus test case – DCOPF optimal transmission switching problem

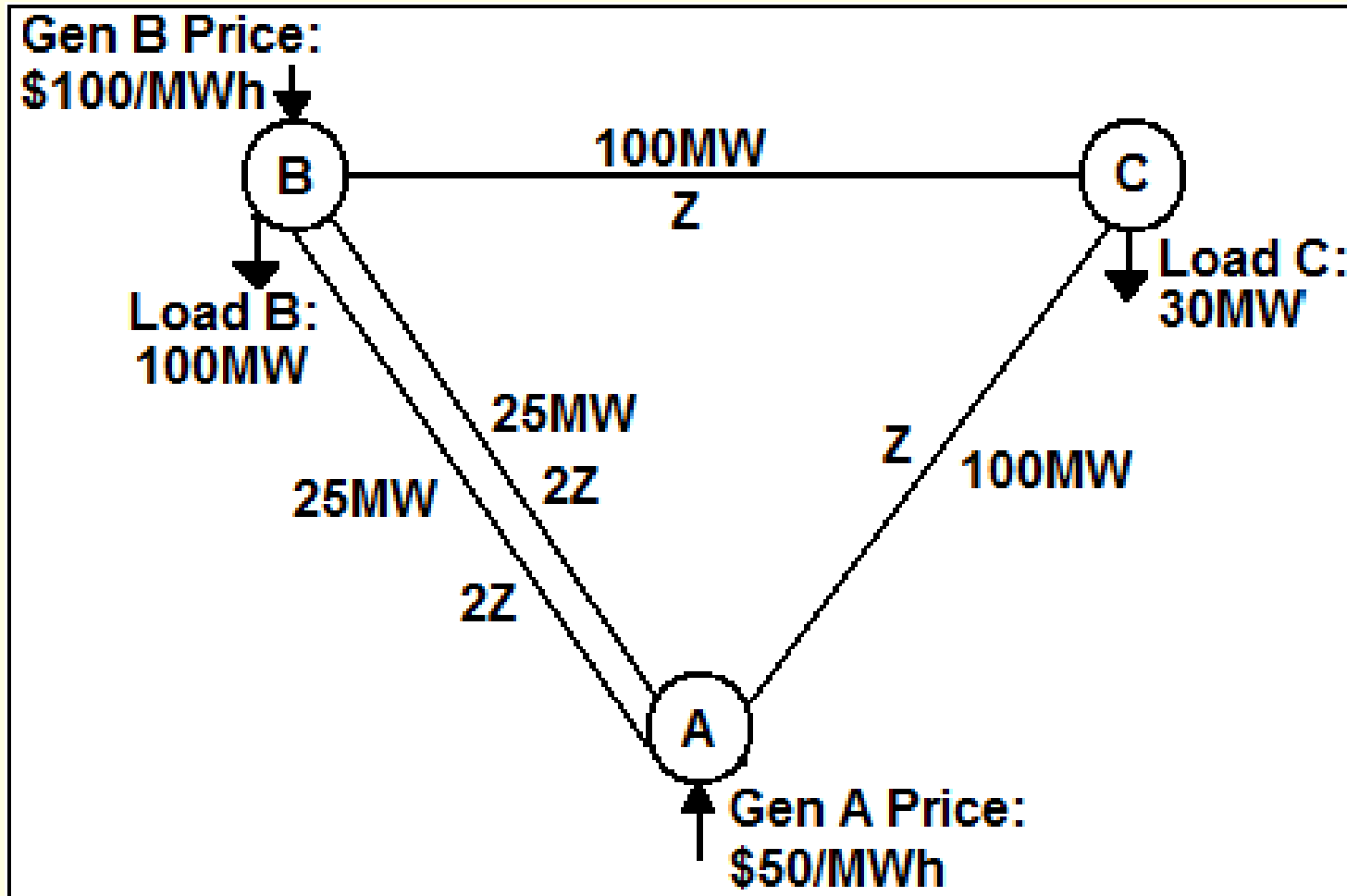


# Overview of Financial Transmission Rights

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- FTRs are used to hedge price risk
- FTR settlements are financed by congestion rents
- Revenue inadequacy occurs when ISO does not collect enough congestion rent to fulfill its obligation to FTR holders
  - ISO may then allocate shortfall to participants or carry it forward and try to recover it from surplus at other times
- Revenue adequacy of FTRs is guaranteed for the static DC topology (since the simultaneous FTR feasible solution corresponds to a suboptimal feasible power flow)
- Revenue adequacy is not guaranteed if the network topology changes
  - Optimal transmission switching undermines the assumption of a static topology

# 3-Bus FTR Revenue Adequacy Example





# Revenue Inadequacy due to Transmission Switching

3-bus example C optimal dispatch results (no switching)

Bus:	Gen Pg:	LMP:	Gen Cost:	Transaction:	MW:	Cong. Rent:
A	90MW	\$50/MWh	\$4,500	A – B	60MW	\$3,000
B	40MW	\$100/MWh	\$4,000	A – C	30MW	\$750
C	0MW	\$75/MWh	\$0	<b>Total Congestion Rent:</b>		<b>\$3,750</b>
<b>Total Generation Cost:</b>			<b>\$8,500</b>			

3-bus example C optimal dispatch results (lines A-B1 and A-B2 open)

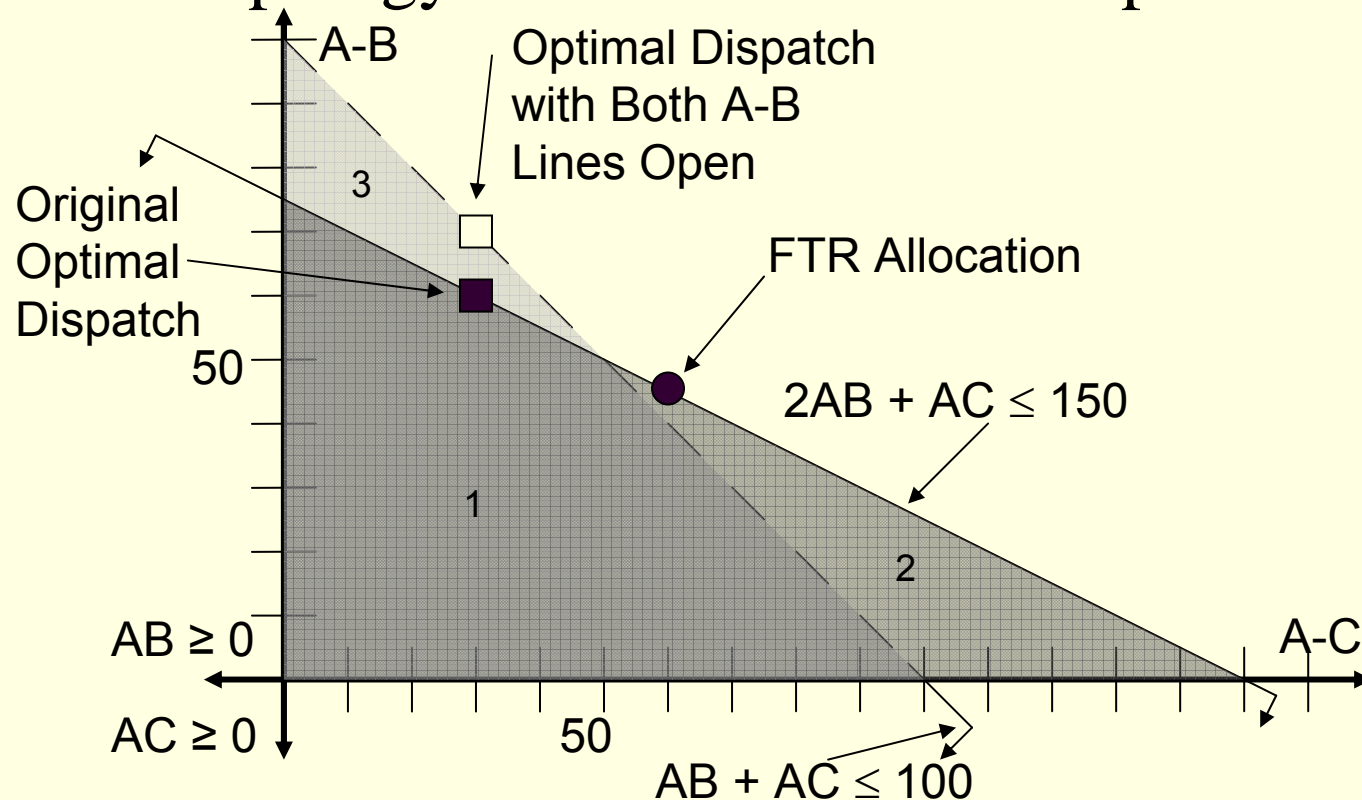
Bus:	Gen Pg:	LMP:	Gen Cost:	Transaction:	MW:	Cong. Rent:
A	100MW	\$50/MWh	\$5,000	A – B	70MW	\$3,500
B	30MW	\$100/MWh	\$3,000	A – C	30MW	\$1,500
C	0MW	\$100/MWh	\$0	<b>Total Congestion Rent:</b>		<b>\$5,000</b>
<b>Total Generation Cost:</b>			<b>\$8,000</b>			

3-bus example C results – FTR settlements

Source to Sink:	FTR Quantity:	FTR Settlements (No Switching):	FTR Settlements (Lines A-B1 and A-B2 Open):
A to B	45MW	\$2,250 (LMP gap: \$50/MWh)	\$2,250 (LMP gap: \$50/MWh)
A to C	60MW	\$1,500 (LMP gap: \$25/MWh)	\$3,000 (LMP gap: \$50/MWh)
<b>Total FTR Settlements:</b>		<b>\$3,750</b>	<b>\$5,250</b>

# Revenue Inadequacy due to Transmission Switching

- FTR allocation is revenue adequate for initial topology but revenue inadequate for optimal network topology with both A-B lines open



# Transmission Switching Can Help Regain Revenue Adequacy

3-bus example C results (line A-B1 failed)

Bus:	Gen Pg:	LMP:	Gen Cost:	Transaction:	MW:	Cong. Rent:
A	65MW	\$50/MWh	\$3,250	A – B	35MW	\$1,750
B	65MW	\$100/MWh	\$6,500	A – C	30MW	\$750
C	0MW	\$75/MWh	\$0	<b>Total Congestion Rent:</b>		<b>\$2,500</b>
<b>Total Generation Cost:</b>			<b>\$9,750</b>			

3-bus example C optimal dispatch results (lines A-B1 failed A-B2 open)

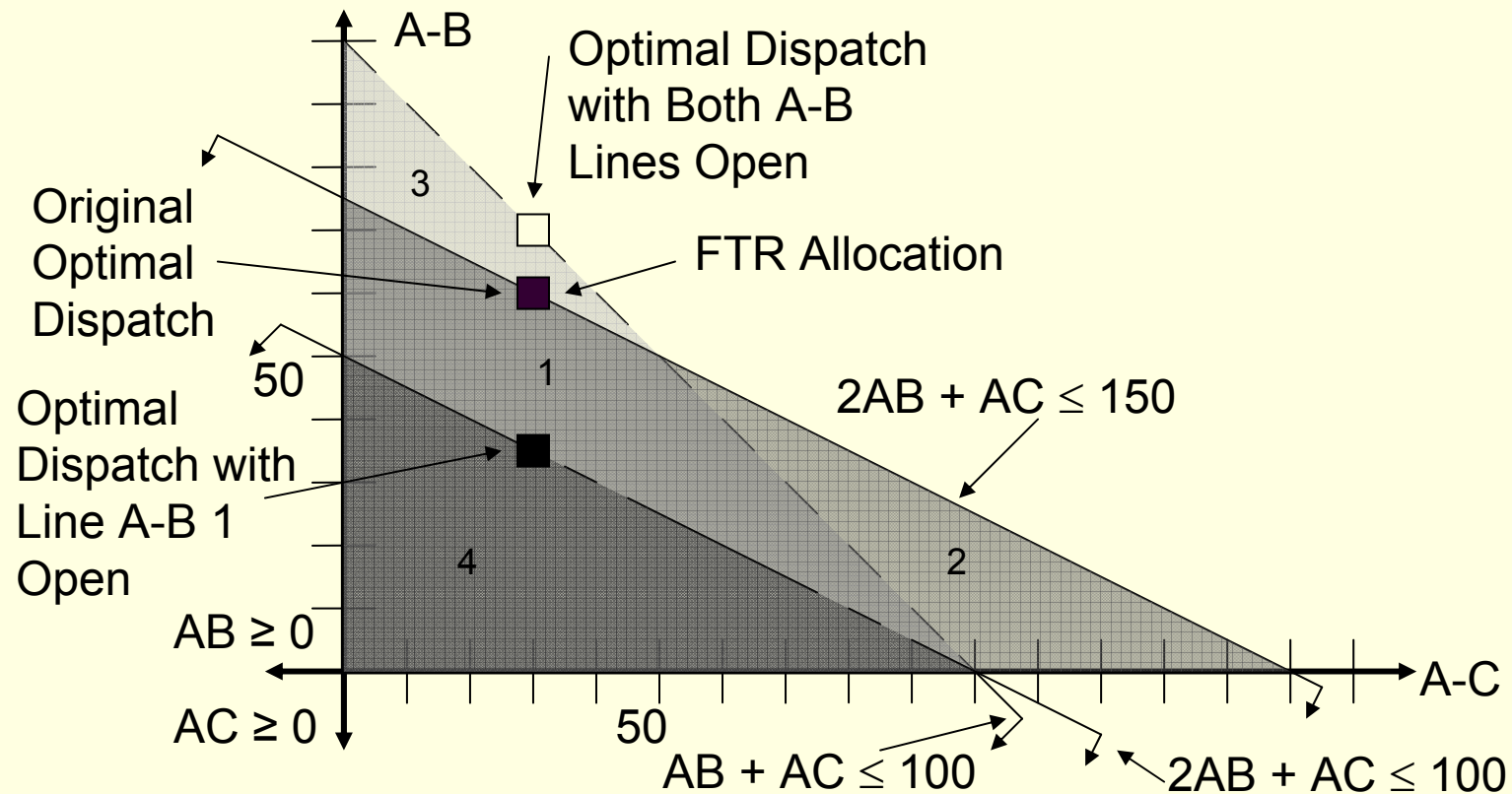
Bus:	Gen Pg:	LMP:	Gen Cost:	Transaction:	MW:	Cong. Rent:
A	100MW	\$50/MWh	\$5,000	A – B	70MW	\$3,500
B	30MW	\$100/MWh	\$3,000	A – C	30MW	\$1,500
C	0MW	\$100/MWh	\$0	<b>Total Congestion Rent:</b>		<b>\$5,000</b>
<b>Total Generation Cost:</b>			<b>\$8,000</b>			

3-bus example C results – FTR settlements (line A-B1 failed)

Source to Sink:	FTR Quantity:	FTR Settlement (No Switching):	FTR Settlement (Line A-B2 Opened):
A to B	60MW	\$3,000 (LMP gap: \$50/MWh)	\$3,000 (LMP gap: \$50/MWh)
A to C	30MW	\$750 (LMP gap: \$25/MWh)	\$750 (LMP gap: \$25/MWh)
<b>Total FTR Settlements:</b>		<b>\$3,750</b>	<b>\$3,750</b>

# Transmission Switching Can Help Regain Revenue Adequacy

- Line outage causes revenue inadequacy (loss of A-B 1)
- Further grid modifications may regain revenue adequacy and improve market surplus (open line A-B 2)



# Policy Implications

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- Optimal transmission switching improves social welfare
  - Yet market participants may object since it can cause revenue inadequacy, affects LMPs, generation rents, congestion rents, etc.
- How to deal with revenue inadequacy?
  - Implement side payments and who pays?
  - De-rate FTR payments?
- Emerging “smart grid” technologies may make certain market mechanisms obsolete
  - Rethink market design principles?
- How would optimal transmission switching affect FTR auctions?

# Summary

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- FTRs are important as they are used to hedge price risk
- Revenue adequacy of FTRs is vulnerable to grid topology changes
- Co-optimizing generation and network topology improves market surplus even while maintaining reliability criteria
  - Unfortunately, it undermines prevailing market mechanisms
  - Can cause revenue inadequacy in FTR markets
  - It has unpredictable distributional effects on market participants

**QUESTIONS?**  
**Thank you!**

<http://www.ieor.berkeley.edu/~oren/index.htm>



# Publications

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## Journal Papers:

- [1] K. W. Hedman, R. P. O'Neill, E. B. Fisher, and S. S. Oren, "Optimal transmission switching – sensitivity analysis and extensions," *IEEE Trans. Power Syst.*, vol. 23, no. 3, pp. 1469-1479, Aug. 2008.
- [2] K. W. Hedman, R. P. O'Neill, E. B. Fisher, and S. S. Oren, "Optimal transmission switching with contingency analysis," *IEEE Trans. Power Syst.*, vol. 24, no. 3, Aug. 2009.
- [3] K. W. Hedman, M. C. Ferris, R. P. O'Neill, E. B. Fisher, and S. S. Oren, "Co-optimization of generation unit commitment and transmission switching with N-1 reliability," *IEEE Trans. Power Syst.*, accepted for publication.
- [4] R. P. O'Neill, K. W. Hedman, E. A. Krall, A. Papavasiliou, M. C. Ferris, E. B. Fisher, and S. S. Oren, "Economic analysis of the N-1 reliable unit commitment and transmission switching problem using duality concepts," *Energy Systems*, accepted for publication.



# Publications cont'd

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## Under Review:

- [5] K. W. Hedman, R. P. O'Neill, E. B. Fisher, and S. S. Oren, "Smart flexible just-in-time transmission and flowgate bidding," *IEEE Trans. Power Syst.*, Submitted June 1, 2009; Revised November 15, 2009.

## Peer-Reviewed Conference Publications:

- [6] K. W. Hedman, R. P. O'Neill, and S. S. Oren, "Analyzing valid inequalities of the generation unit commitment problem," in *Proc. Power Syst. Conf. and Expo.*, March 2009.
- [7] E. B. Fisher, K. W. Hedman, R. P. O'Neill, M. C. Ferris, and S. S. Oren, "Optimal transmission switching in electric networks for improved economic operations," in *INFRADAY Conference 2008*.